Automatic Image Alignment, Part 2



with a lot of slides stolen from Steve Seitz and Rick Szeliski CS180: Intro to Comp. Vision and Comp. Photo Alexei Efros, UC Berkeley, Fall 2024

Feature Detection



Feature Matching

How do we match the features between the images?

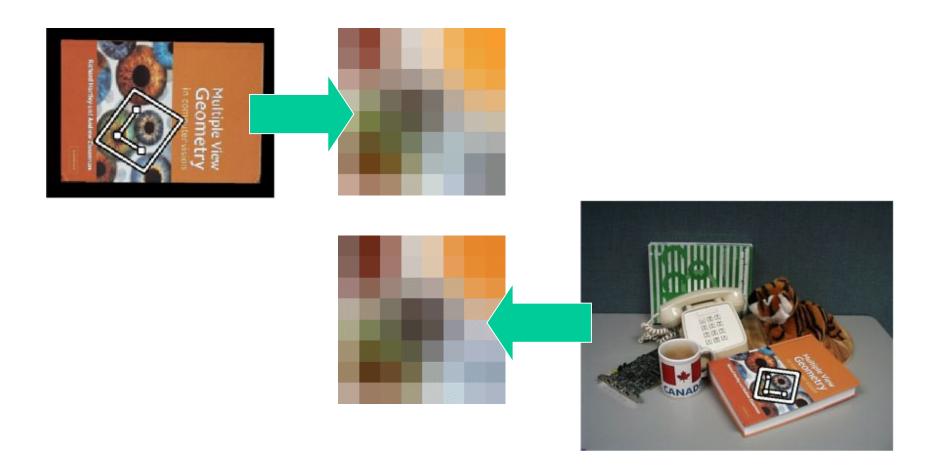
- Need a way to <u>describe</u> a region around each feature
 - e.g. image patch around each feature
- Use successful matches to estimate homography
 - Need to do something to get rid of outliers

Issues:

- What if the image patches for several interest points look similar?
 - Make patch size bigger
- What if the image patches for the same feature look different due to scale, rotation, etc.
 - Need an invariant descriptor

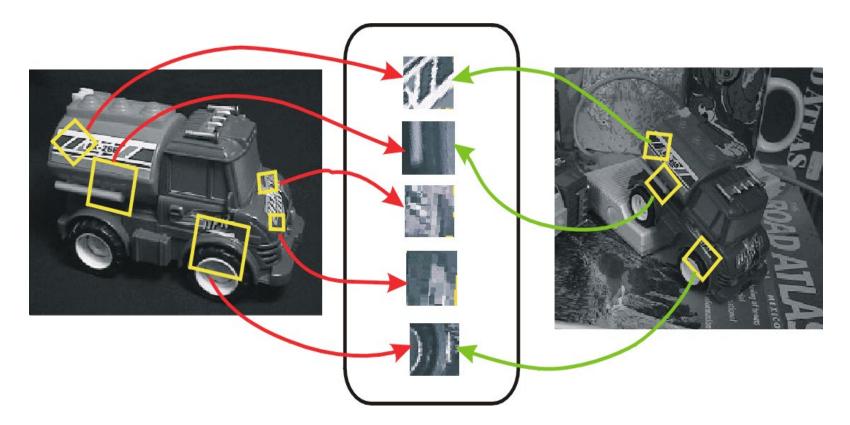
Invariant Feature Descriptors

Schmid & Mohr 1997, Lowe 1999, Baumberg 2000, Tuytelaars & Van Gool 2000, Mikolajczyk & Schmid 2001, Brown & Lowe 2002, Matas et. al. 2002, Schaffalitzky & Zisserman 2002



Invariant Local Features

Image content is transformed into local feature coordinates that are invariant to translation, rotation, scale, and other imaging parameters



Features Descriptors

Applications

Feature points are used for:

- Image alignment (homography, fundamental matrix)
- 3D reconstruction
- Motion tracking
- Object recognition
- Indexing and database retrieval
- Robot navigation
- ... other

Today's lecture

- 1 Feature <u>detector</u>
 - scale invariant Harris corners
- 1 Feature descriptor
 - patches, oriented patches

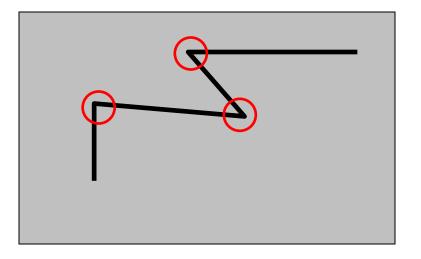
Reading:

Multi-image Matching using Multi-scale image patches, CVPR 2005

Feature Detector – Harris Corner

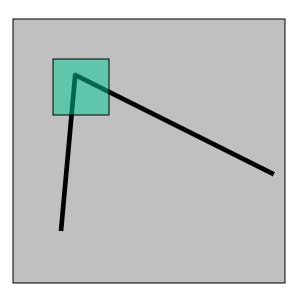
Harris corner detector

C.Harris, M.Stephens. "A Combined Corner and Edge Detector". 1988

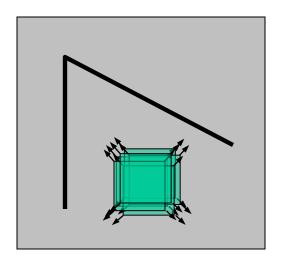


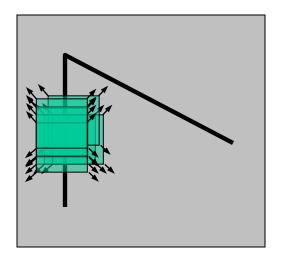
We should easily recognize the point by looking through a small window Shifting a window in *any direction* should give *a large*

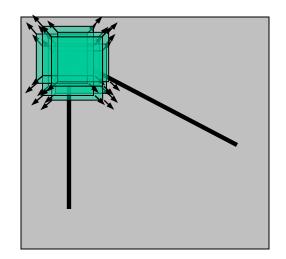
change in intensity



Harris Detector: Basic Idea







"flat" region: no change in all directions

"edge":

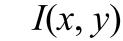
no change along the edge direction

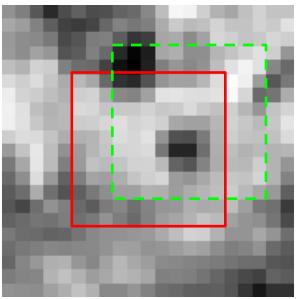
"corner":

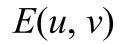
significant change in all directions

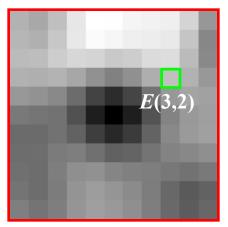
Change in appearance of window W for the shift [u,v]:

$$E(u,v) = \sum_{(x,y)\in W} [I(x+u, y+v) - I(x, y)]^2$$



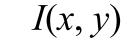


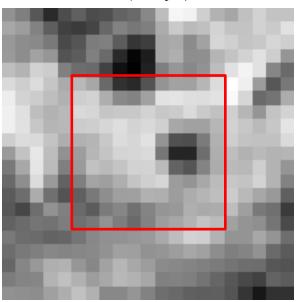


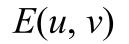


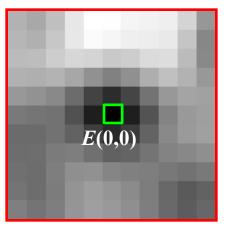
Change in appearance of window W for the shift [u,v]:

$$E(u,v) = \sum_{(x,y)\in W} [I(x+u, y+v) - I(x, y)]^2$$





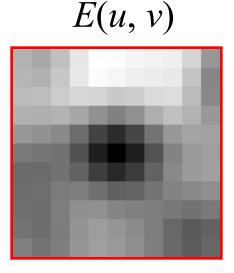




Change in appearance of window W for the shift [u,v]:

$$E(u,v) = \sum_{(x,y)\in W} [I(x+u, y+v) - I(x, y)]^2$$

We want to find out how this function behaves for small shifts



First-order Taylor approximation for small motions [*u*, *v*]:

 $I(x+u, y+v) = I(x, y) + I_x u + I_y v + \text{higher order terms}$ $\approx I(x, y) + I_x u + I_y v$ $= I(x, y) + \begin{bmatrix} I_x & I_y \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix}$

• Let's plug this into

$$E(u,v) = \sum_{(x,y)\in W} [I(x+u, y+v) - I(x, y)]^2$$

$$E(u,v) = \sum_{(x,y)\in W} [I(x+u, y+v) - I(x,y)]^2$$

$$\approx \sum_{(x,y)\in W} [I(x,y) + \begin{bmatrix} I_x & I_y \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} - I(x,y)]^2$$

$$= \sum_{(x,y)\in W} \left(\begin{bmatrix} I_x & I_y \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix} \right)^2$$

$$= \sum_{(x,y)\in W} \begin{bmatrix} u & v \end{bmatrix} \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix}$$

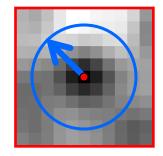
The quadratic approximation simplifies to

$$E(u,v) \approx \begin{bmatrix} u & v \end{bmatrix} M \begin{bmatrix} u \\ v \end{bmatrix}$$

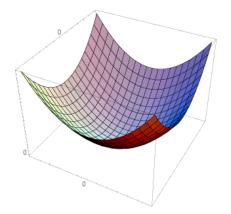
where *M* is a second moment matrix computed from image derivatives:

$$M = \sum_{(x,y)\in W} \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

- The surface E(u,v) is locally approximated by a quadratic form. Let's try to understand its shape.
 - Specifically, in which directions does it have the smallest/greatest change?



$$E(u,v) \approx \begin{bmatrix} u & v \end{bmatrix} M \begin{bmatrix} u \\ v \end{bmatrix}$$
$$M = \sum_{(x,y)\in W} \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix}$$

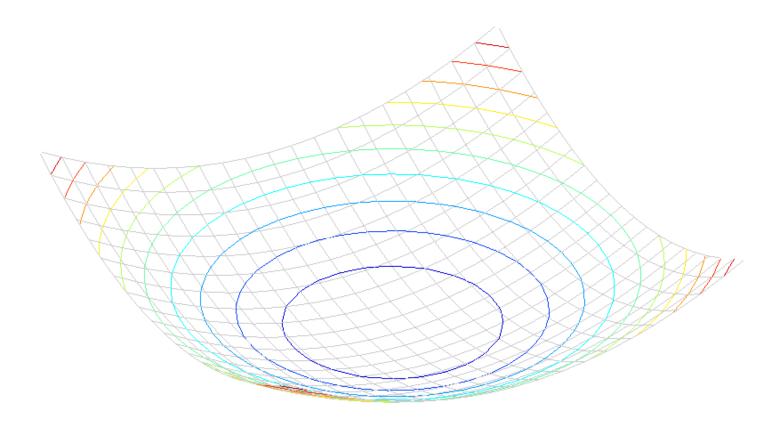


First, consider the axis-aligned case (gradients are either horizontal or vertical)

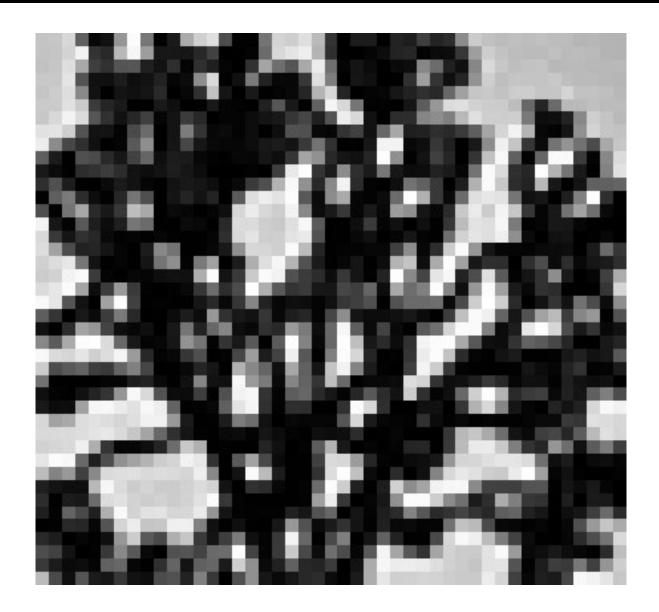
$$M = \sum_{(x,y)\in W} \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix} = \begin{bmatrix} a & 0 \\ 0 & b \end{bmatrix}$$

If either *a* or *b* is close to 0, then this is **not** a corner, so look for locations where both are large.

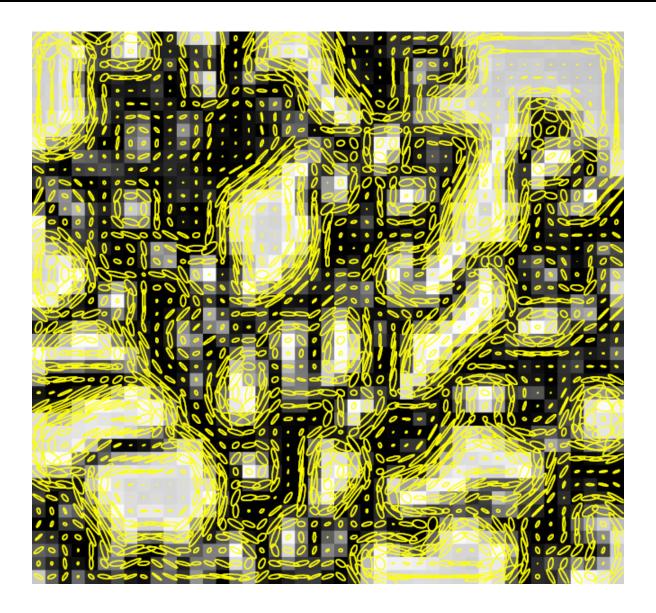
Consider a horizontal "slice" of E(u, v): $\begin{bmatrix} u & v \end{bmatrix} M \begin{bmatrix} u \\ v \end{bmatrix} = \text{const}$ This is the equation of an ellipse.



Visualization of second moment matrices



Visualization of second moment matrices

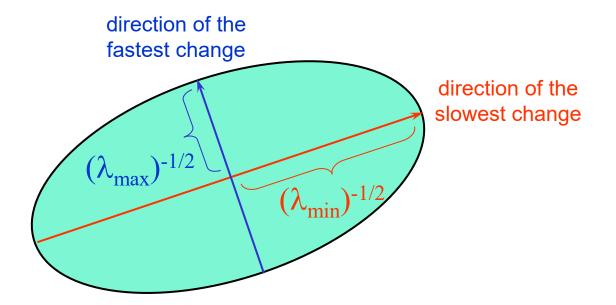


Consider a horizontal "slice" of E(u, v): $\begin{bmatrix} u & v \end{bmatrix} M \begin{bmatrix} u \\ v \end{bmatrix} = \text{const}$

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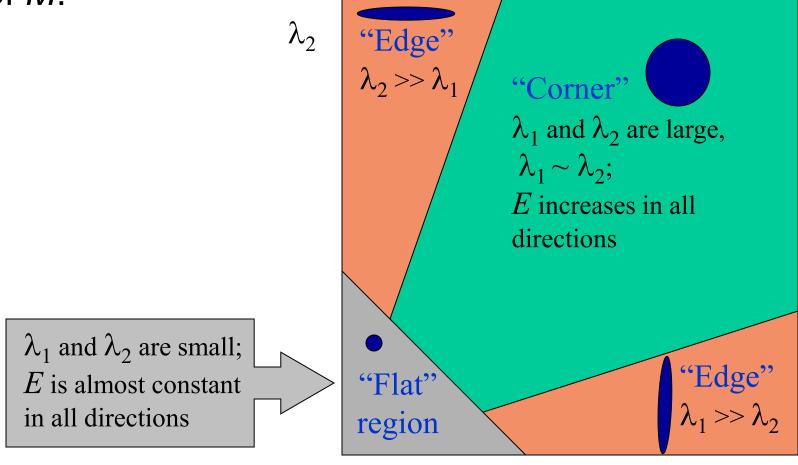
Diagonalization of M:
$$M = R^{-1} \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} R$$

The axis lengths of the ellipse are determined by the eigenvalues and the orientation is determined by R



Interpreting the eigenvalues

Classification of image points using eigenvalues of *M*:



Measure of corner response:

$$R = \frac{\det M}{\operatorname{Trace} M}$$

$$\det M = \lambda_1 \lambda_2$$

trace $M = \lambda_1 + \lambda_2$

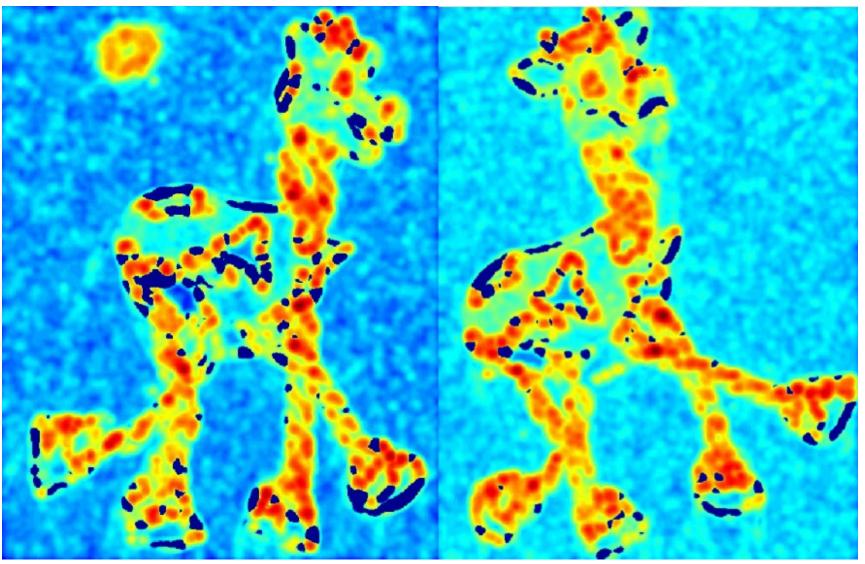
Harris detector: Steps

- 1. Compute Gaussian derivatives at each pixel
- 2. Compute second moment matrix *M* in a Gaussian window around each pixel
- 3. Compute corner response function *R*
- 4. Threshold *R*
- 5. Find local maxima of response function (nonmaximum suppression)

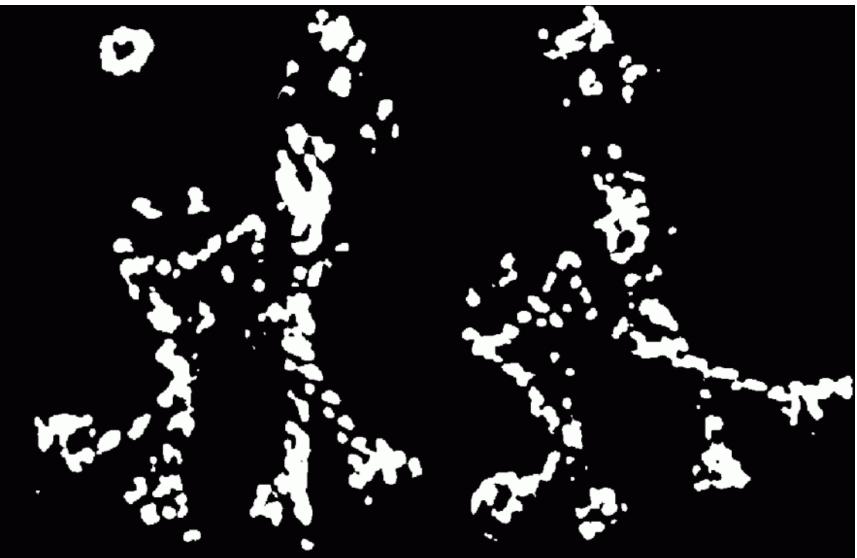
C.Harris and M.Stephens. <u>"A Combined Corner and Edge Detector.</u>" *Proceedings of the 4th Alvey Vision Conference*: pages 147—151, 1988.



Compute corner response R



Find points with large corner response: *R*>threshold



Take only the points of local maxima of R

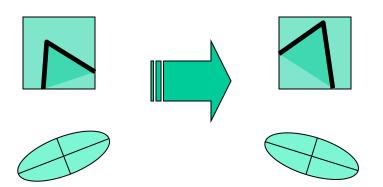
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Harris Detector: Some Properties

Rotation invariance



Ellipse rotates but its shape (i.e. eigenvalues) remains the same

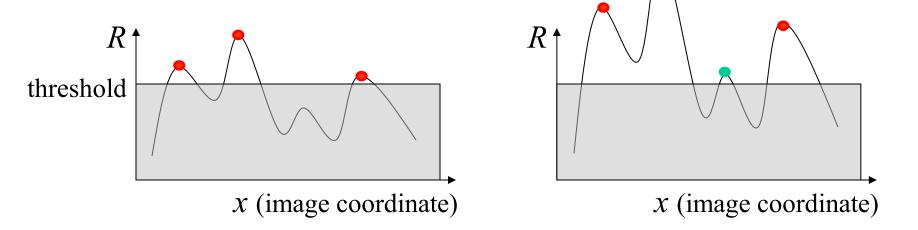
Corner response R is invariant to image rotation

Harris Detector: Some Properties

Partial invariance to affine intensity change

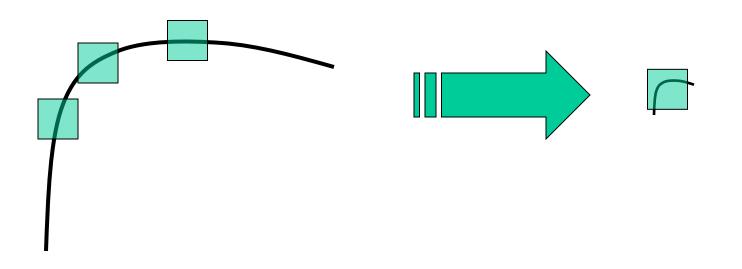
✓ Only derivatives are used => invariance to intensity shift $I \rightarrow I + b$

✓ Intensity scale: $I \rightarrow a I$



Harris Detector: Some Properties

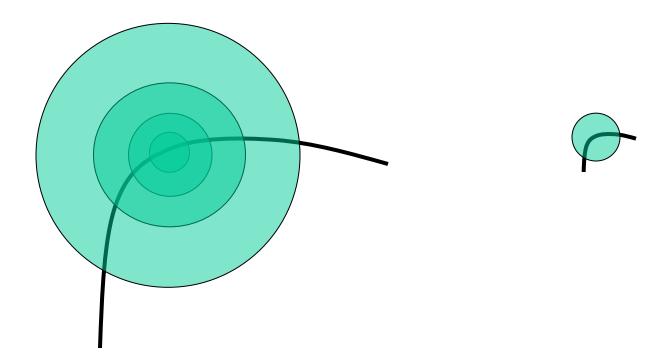
But: non-invariant to *image scale*!



Corner !

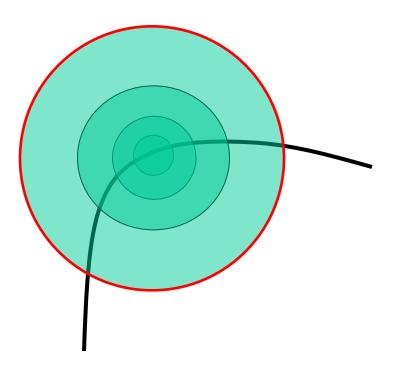
All points will be classified as edges

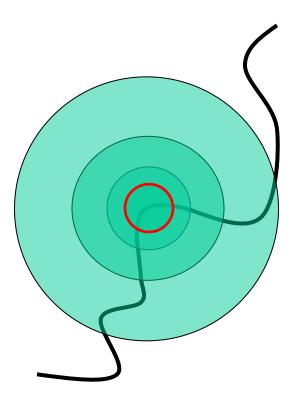
Consider regions (e.g. circles) of different sizes around a point Regions of corresponding sizes will look the same in both images



The problem: how do we choose corresponding circles *independently* in each image?

Choose the scale of the "best" corner





Feature selection

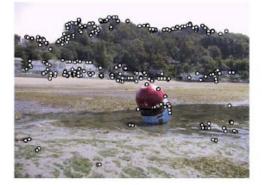
Distribute points evenly over the image



Adaptive Non-maximal Suppression

Desired: Fixed # of features per image

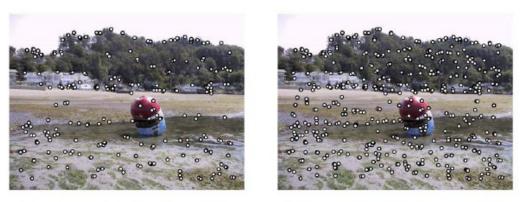
- Want evenly distributed spatially...
- Sort points by non-maximal suppression radius [Brown, Szeliski, Winder, CVPR'05]



(a) Strongest 250



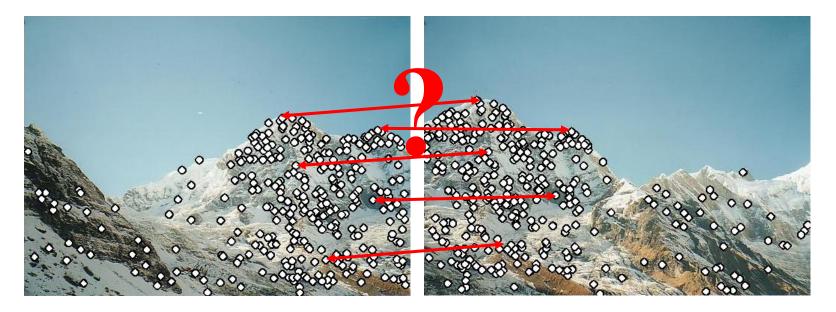
(b) Strongest 500



(c) ANMS 250, r = 24

Feature descriptors

We know how to detect points Next question: **How to match them?**



Point descriptor should be:

1. Invariant

2. Distinctive

Feature Descriptor – MOPS

Multi-Scale Oriented Patches

Interest points

- Multi-scale Harris corners
- Orientation from blurred gradient
- Geometrically invariant to rotation

Descriptor vector

- Bias/gain normalized sampling of local patch (8x8)
- Photometrically invariant to affine changes in intensity

[Brown, Szeliski, Winder, CVPR'2005]

Detect Features, setup Frame

Orientation = blurred gradient

Rotation Invariant Frame

• Scale-space position (x, y, s) + orientation (θ)



Detections at multiple scales

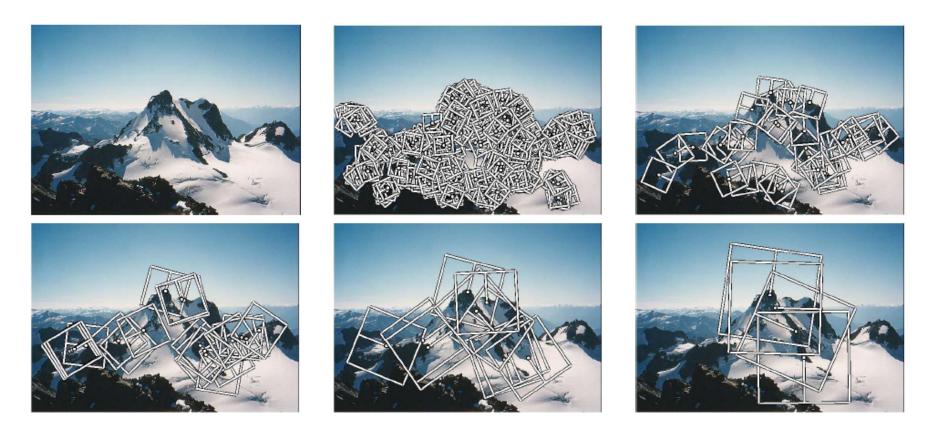


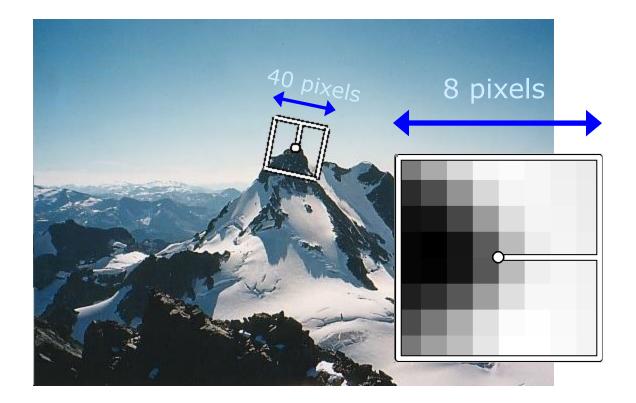
Figure 1. Multi-scale Oriented Patches (MOPS) extracted at five pyramid levels from one of the Matier images. The boxes show the feature orientation and the region from which the descriptor vector is sampled.

MOPS descriptor vector

8x8 oriented patch

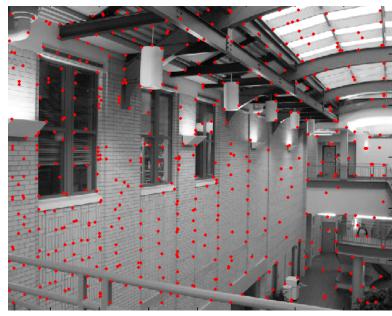
• Sampled at 5 x scale

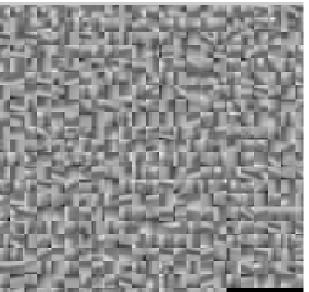
Bias/gain normalisation: I' = $(I - \mu)/\sigma$

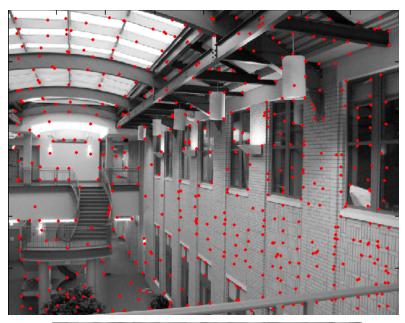


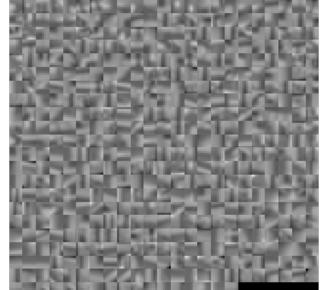
Automatic Feature Matching

Feature matching







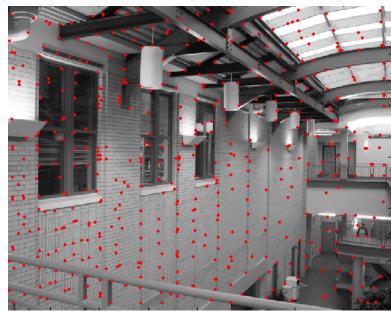


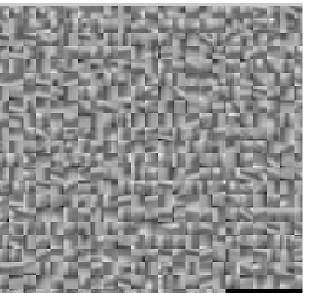
?

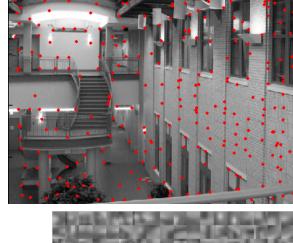
Feature matching

- Pick best match!
 - For every patch in image 1, find the most similar patch (e.g. by L2 distance).
 - Called "nearest neighbor" in machine learning
- Can do various speed ups:
 - Hashing
 - compute a short descriptor from each feature vector, or hash longer descriptors (randomly)
 - Fast Nearest neighbor techniques
 - kd-trees and their variants
 - Clustering / Vector quantization
 - So called "visual words"

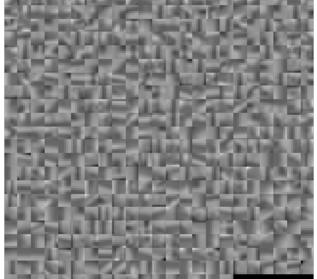
What about outliers?







?

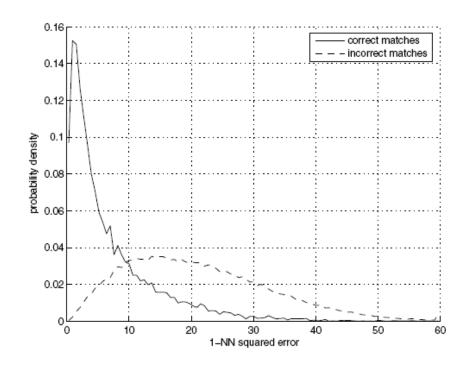


Feature-space outlier rejection

Let's not match all features, but only these that have "similar enough" matches?

How can we do it?

- SSD(patch1,patch2) < threshold
- How to set threshold?



Feature-space outlier rejection: symmetry

Let's not match all features, but only these that have "similar enough" matches?

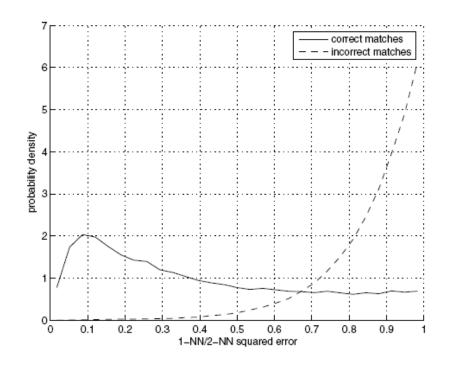
How can we do it?

• Symmetry: x's NN is y, and y's NN is x

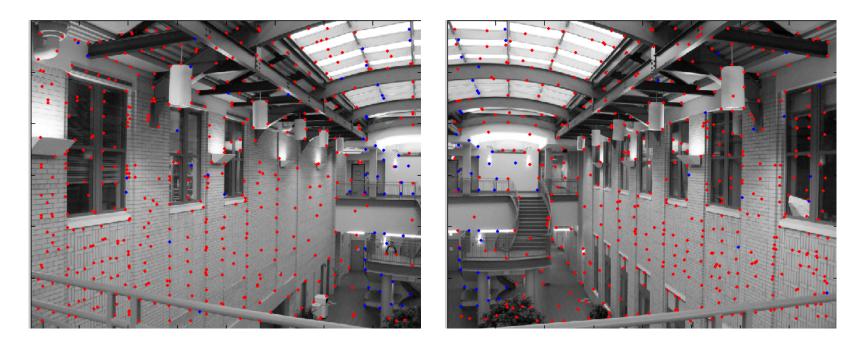
Feature-space outlier rejection: Lowe's trick

A better way [Lowe, 1999]:

- 1-NN: L2 of the closest match
- 2-NN: L2 of the second-closest match
- Look at how much better 1-NN is than 2-NN, e.g. 1-NN/2-NN
- That is, is our best match so much better than the rest?



Feature-space outliner rejection



Can we now compute H from the blue points?

- No! Still too many outliers...
- What can we do?