

# Convolution and Image Derivatives

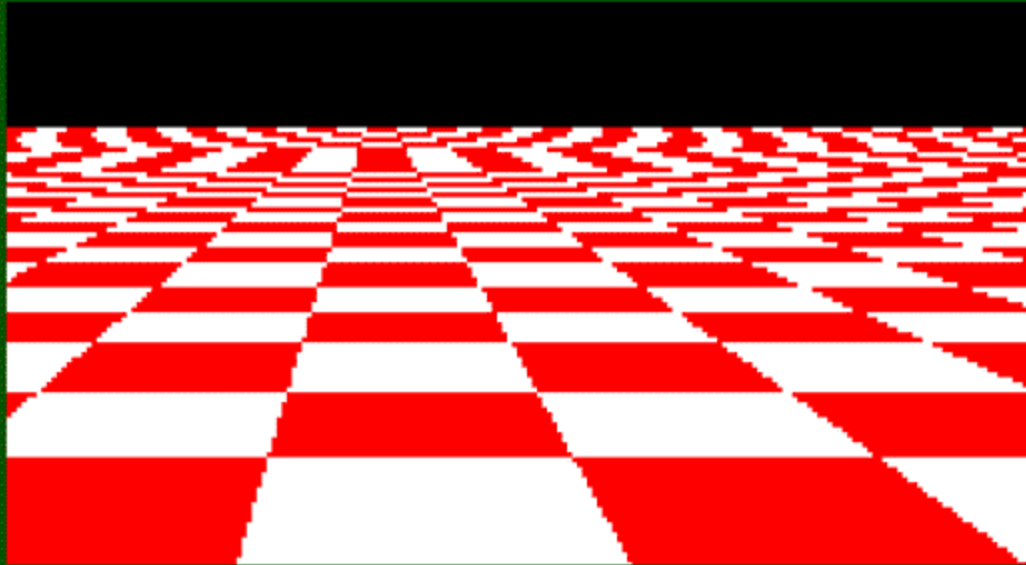
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CS180: Intro to Comp. Vision and Comp. Photo  
Efros & Kanazawa, UC Berkeley, Fall 2025

# Aliasing in images

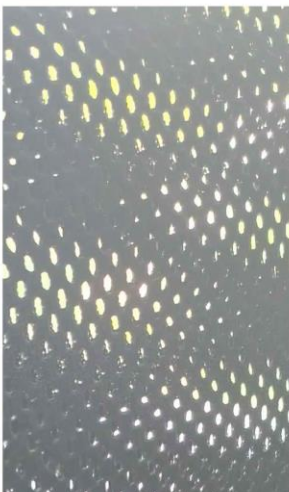
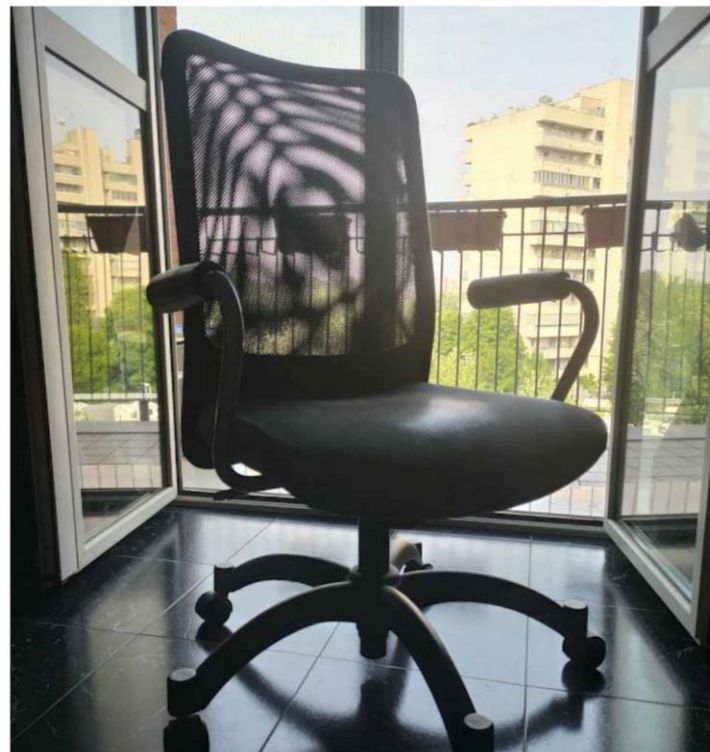
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**Disintegrating textures**

# Aliasing in real images

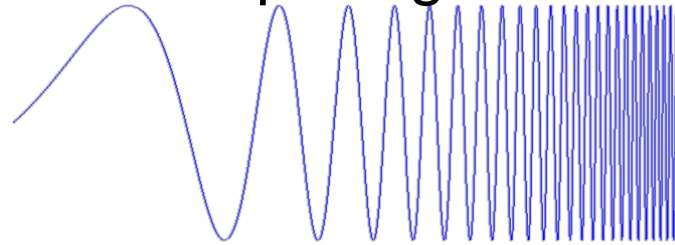
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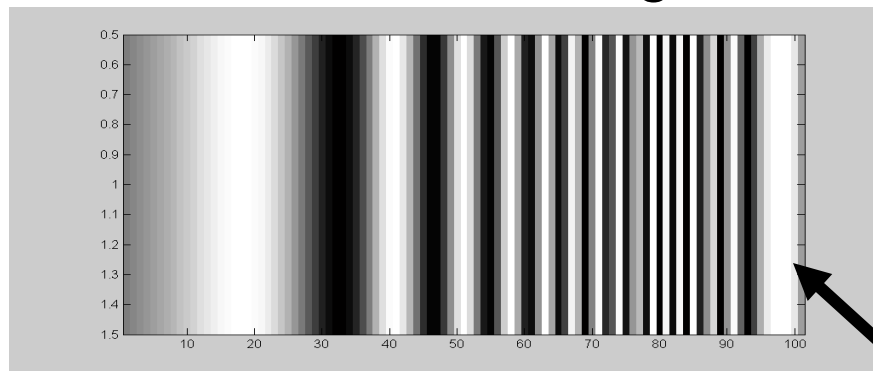
# What's happening?

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Input signal:



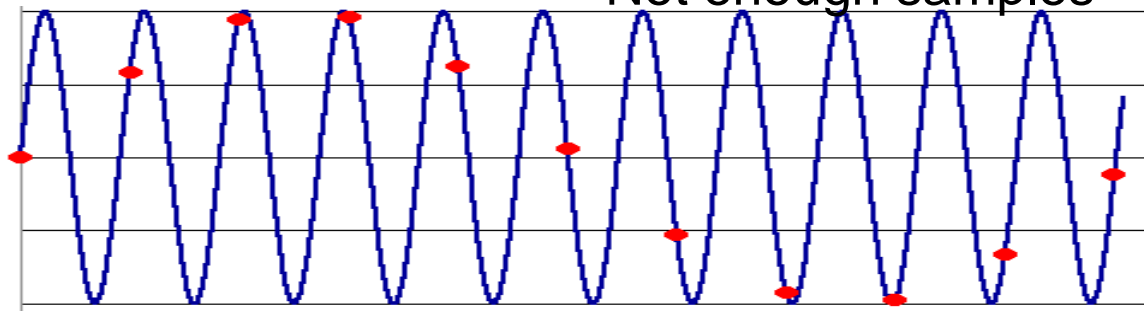
Plot as image:



$x = 0:.05:5$ ; `imagesc(sin((2.^x).*x))`

Alias!

Not enough samples



# Antialiasing

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What can we do about aliasing?

Sample more often

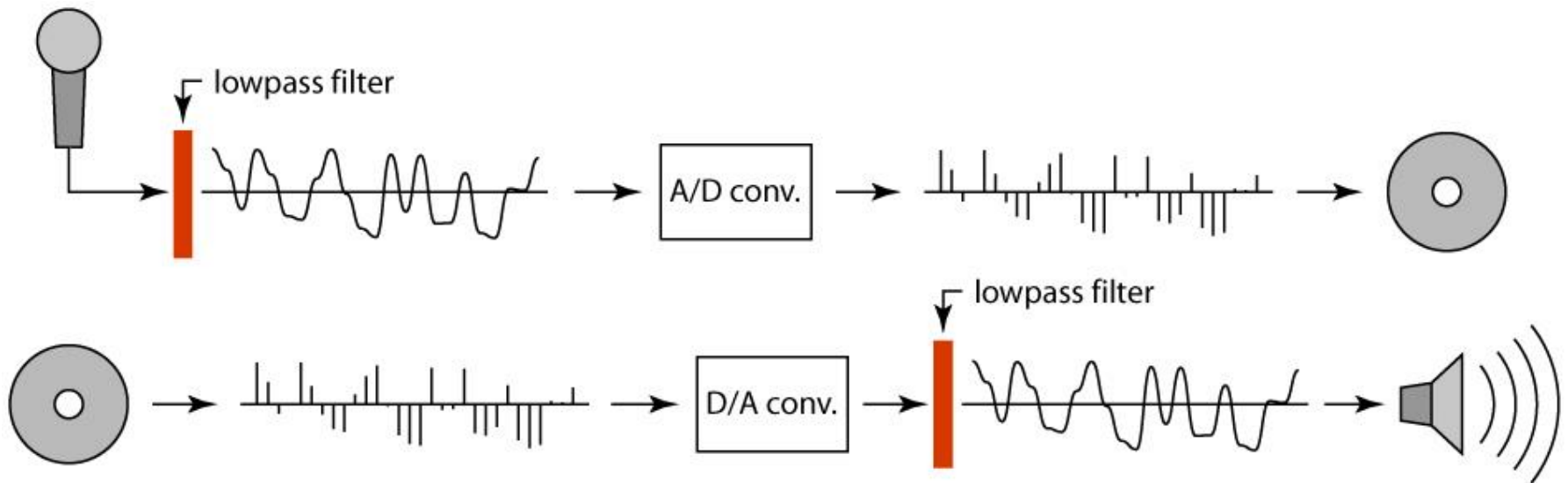
- Join the Mega-Pixel craze of the photo industry
- But this can't go on forever

Make the signal less “wiggly”

- Get rid of some high frequencies
- Will lose information
- But it's better than aliasing

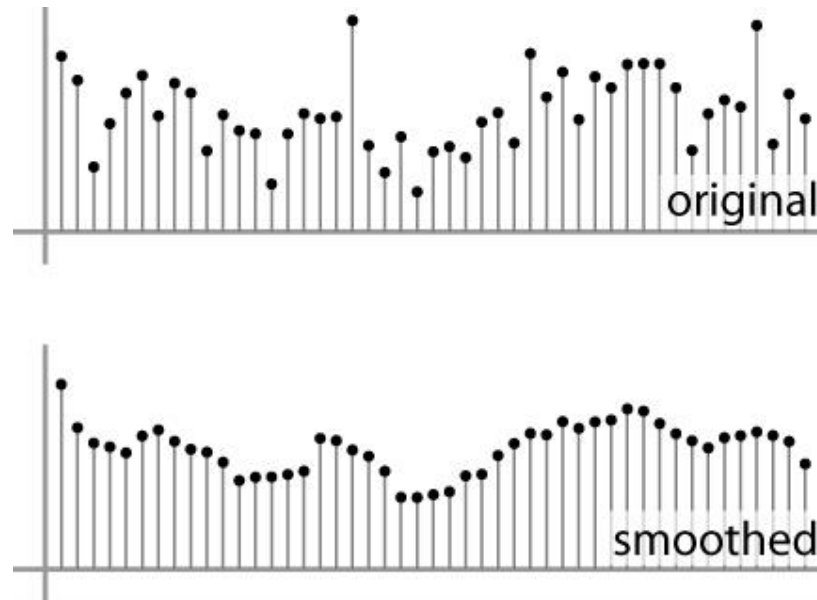
# Preventing aliasing

- Introduce **lowpass filters**:
  - remove high frequencies leaving only safe, low frequencies
  - choose lowest frequency in reconstruction (disambiguate)



# Moving Average

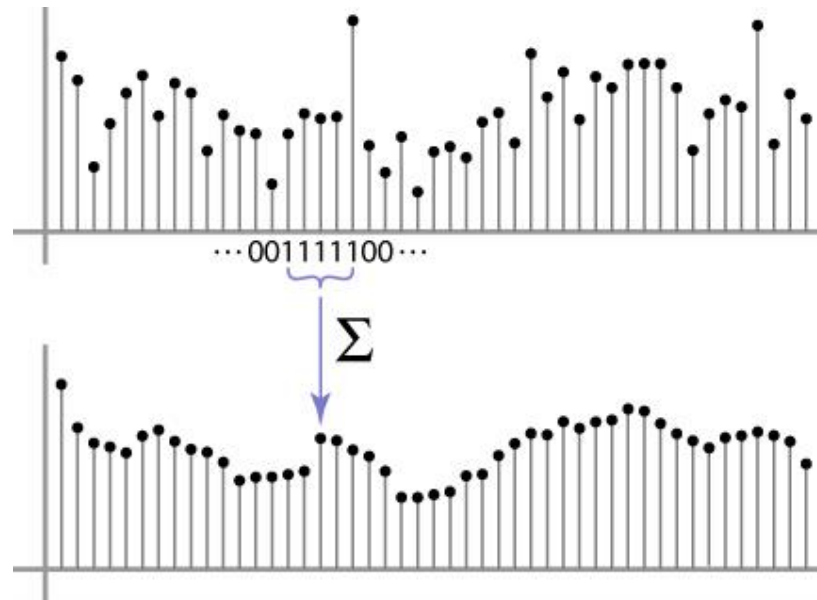
- basic idea: define a new function by averaging over a sliding window
- a simple example to start off: smoothing





# Moving Average

- Can add weights to our moving average
- *Weights* [..., 0, 1, 1, 1, 1, 1, 0, ...] / 5





# In 2D: box filter

$$\frac{1}{9} h[\cdot, \cdot]$$

1	1	1
1	1	1
1	1	1

# Image filtering

$$h[\cdot, \cdot] \frac{1}{9}$$

1	1	1
1	1	1
1	1	1

$f[\cdot, \cdot]$

0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	90	0	90	90	90	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0

$g[\cdot, \cdot]$


$$g[m, n] = \sum_{k, l} h[k, l] f[m + k, n + l]$$

# Image filtering

$$h[\cdot, \cdot] \frac{1}{9}$$

1	1	1
1	1	1
1	1	1

$f[\cdot, \cdot]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

$g[\cdot, \cdot]$

	0	10							

$$g[m, n] = \sum_{k, l} h[k, l] f[m + k, n + l]$$

# Image filtering

$$h[\cdot, \cdot] \frac{1}{9}$$

1	1	1
1	1	1
1	1	1

$f[\cdot, \cdot]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

$g[\cdot, \cdot]$

	0	10	20						

# Image filtering

$$h[\cdot, \cdot] \frac{1}{9}$$

1	1	1
1	1	1
1	1	1

$f[\cdot, \cdot]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

$g[\cdot, \cdot]$

	0	10	20	30					

# Image filtering

$$h[\cdot, \cdot] \frac{1}{9}$$

1	1	1
1	1	1
1	1	1

$f[\cdot, \cdot]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

$g[\cdot, \cdot]$

	0	10	20	30	30				

# Image filtering

$$h[\cdot, \cdot] \frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

$$f[\cdot, \cdot]$$

[illegible]

$$g[\cdot, \cdot]$$

[illegible]



# Image filtering

$$h[\cdot, \cdot] \frac{1}{9}$$

1	1	1
1	1	1
1	1	1

$f[\cdot, \cdot]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

$g[\cdot, \cdot]$

	0	10	20	30	30				
						?			
				50					

# Image filtering

$$h[\cdot, \cdot] \frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

$$f[\cdot, \cdot]$$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

$$g[\cdot, \cdot]$$

	0	10	20	30	30	30	20	10	
	0	20	40	60	60	60	40	20	
	0	30	60	90	90	90	60	30	
	0	30	50	80	80	90	60	30	
	0	30	50	80	80	90	60	30	
	0	20	30	50	50	60	40	20	
	10	20	30	30	30	30	20	10	
	10	10	10	0	0	0	0	0	

# Cross-correlation

Let  $F$  be the image,  $H$  be the kernel (of size  $2k+1 \times 2k+1$ ), and  $G$  be the output image

$$G[i, j] = \sum_{u=-k}^k \sum_{v=-k}^k H[u, v] F[i + u, j + v]$$

This is called a **cross-correlation** operation:

$$G = H \otimes F$$

- Can think of as a “dot product” between local neighborhood and kernel for each pixel

# Box Filter

What does it do?

- Replaces each pixel with an average of its neighborhood
- Achieve smoothing effect (remove sharp features)

$$\frac{1}{9} h[\cdot, \cdot]$$

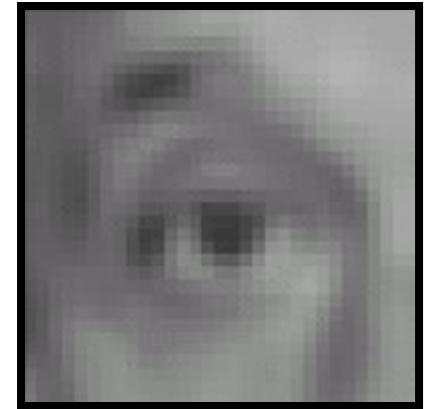
1	1	1
1	1	1
1	1	1

# Linear filters: examples



Original

$$\frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} =$$



Blur (with a mean filter)

# Practice with linear filters



Original

0	0	0
0	1	0
0	0	0

?

# Practice with linear filters



Original

0	0	0
0	1	0
0	0	0



Filtered  
(no change)



# Practice with linear filters



Original

0	0	0
0	0	1
0	0	0

?

# Practice with linear filters



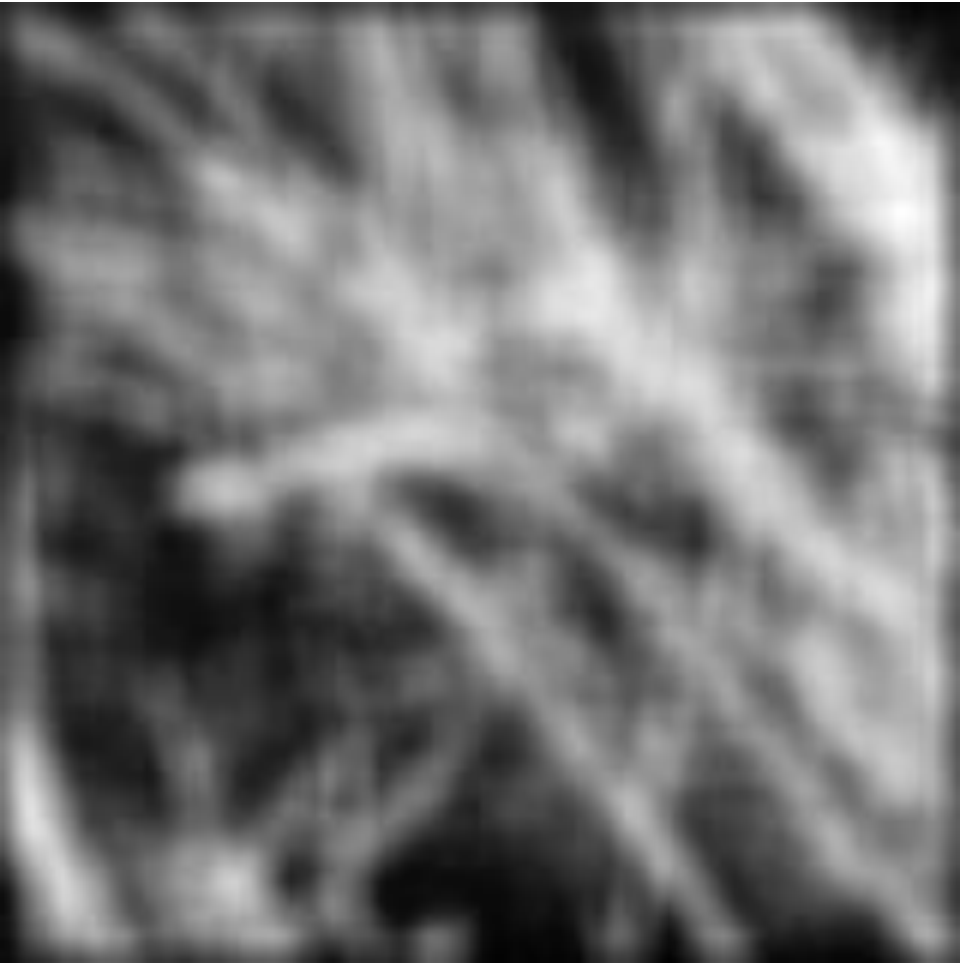
Original

0	0	0
0	0	1
0	0	0



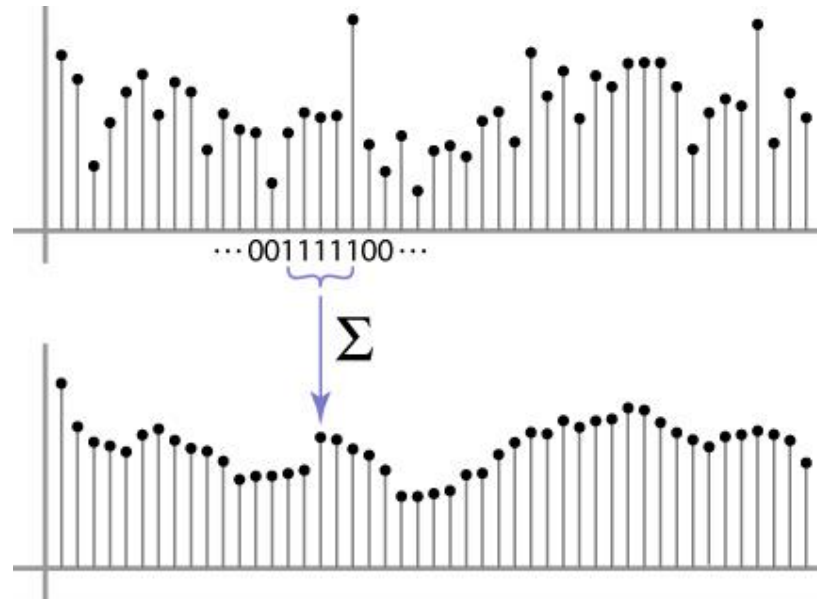
Shifted left  
By 1 pixel

# Back to the box filter



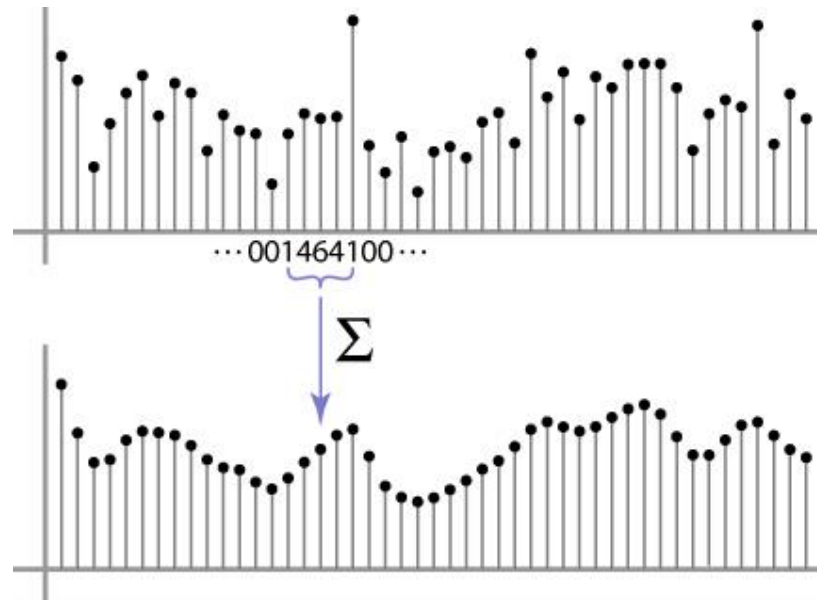
# Moving Average

- Can add weights to our moving average
- *Weights* [..., 0, 1, 1, 1, 1, 1, 0, ...] / 5



# Weighted Moving Average

- bell curve (gaussian-like) weights [..., 1, 4, 6, 4, 1, ...]



# Moving Average In 2D

What are the weights  $H$ ?

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

$F[x, y]$


$H[u, v]$

# Gaussian filtering

A Gaussian kernel gives less weight to pixels further from the center of the window

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

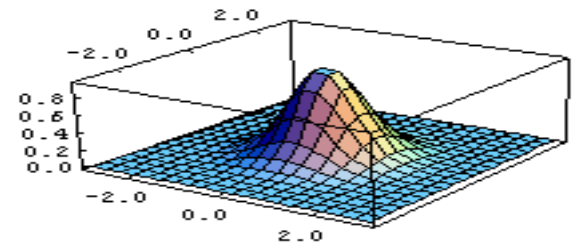
$F[x, y]$

1	2	1
2	4	2
1	2	1

$H[u, v]$

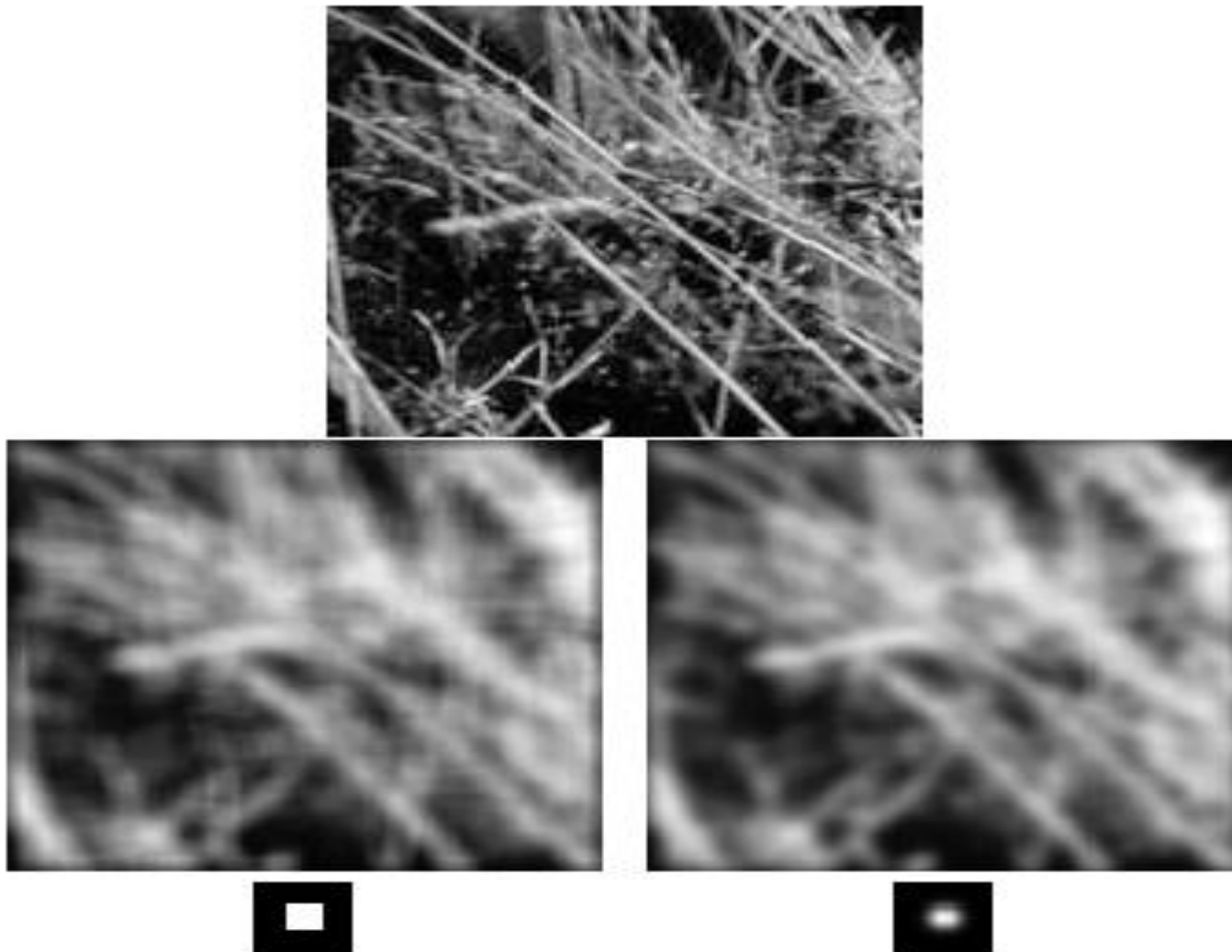
$$h(u, v) = \frac{1}{2\pi\sigma^2} e^{-\frac{u^2+v^2}{\sigma^2}}$$

This kernel is an approximation of a Gaussian function:



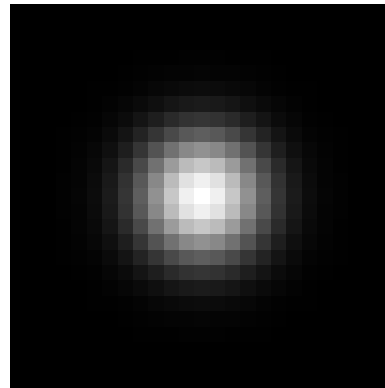
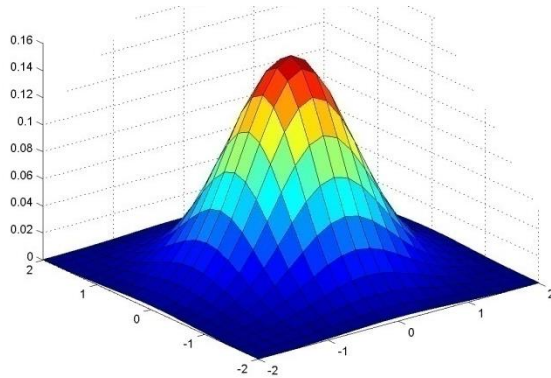


# Mean vs. Gaussian filtering



# Important filter: Gaussian

Weight contributions of neighboring pixels by nearness



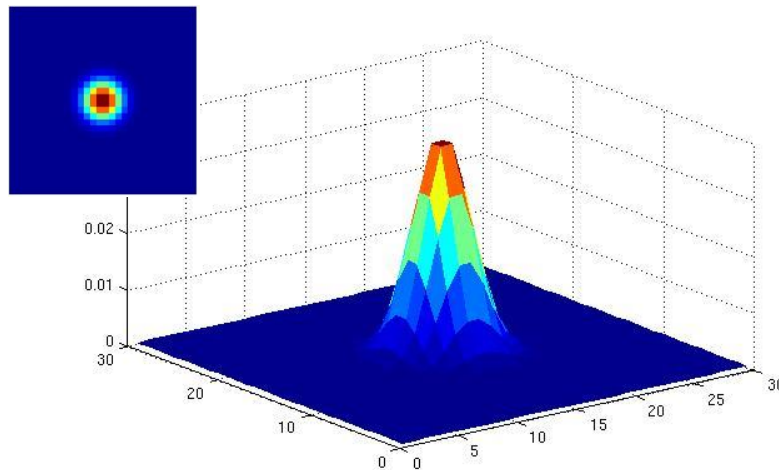
0.003	0.013	0.022	0.013	0.003
0.013	0.059	0.097	0.059	0.013
0.022	0.097	0.159	0.097	0.022
0.013	0.059	0.097	0.059	0.013
0.003	0.013	0.022	0.013	0.003

5 x 5,  $\sigma = 1$

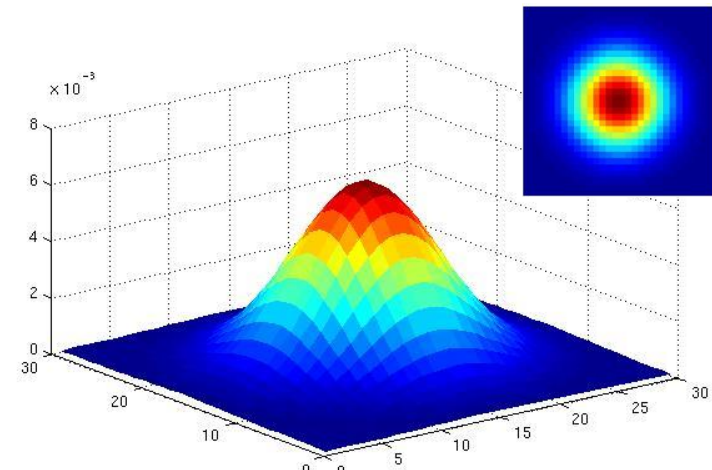
$$G_{\sigma} = \frac{1}{2\pi\sigma^2} e^{-\frac{(x^2+y^2)}{2\sigma^2}}$$

# Gaussian Kernel

$$G_{\sigma} = \frac{1}{2\pi\sigma^2} e^{-\frac{(x^2+y^2)}{2\sigma^2}}$$



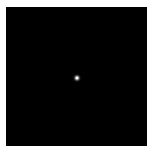
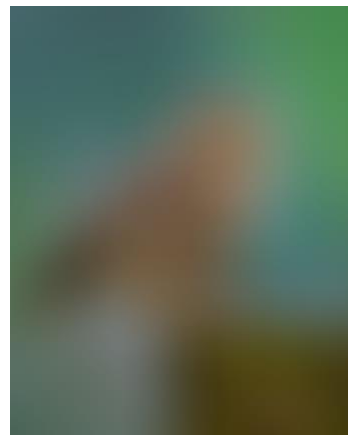
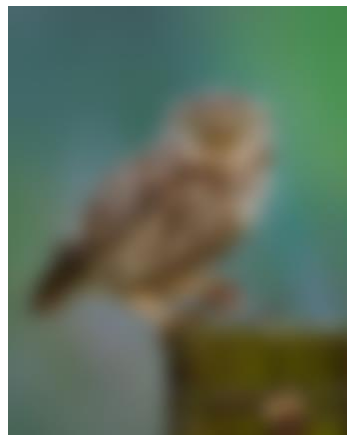
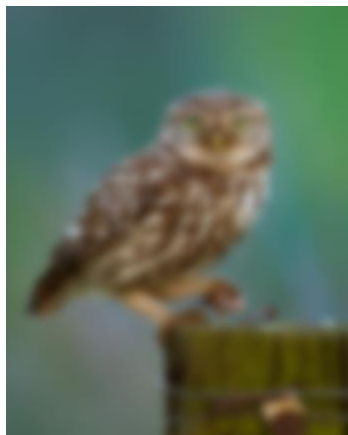
$\sigma = 2$  with  $30 \times 30$   
kernel



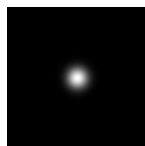
$\sigma = 5$  with  $30 \times 30$   
kernel

- Standard deviation  $\sigma$ : determines extent of smoothing

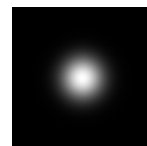
# Gaussian filters



$\sigma = 1$  pixel



$\sigma = 5$  pixels



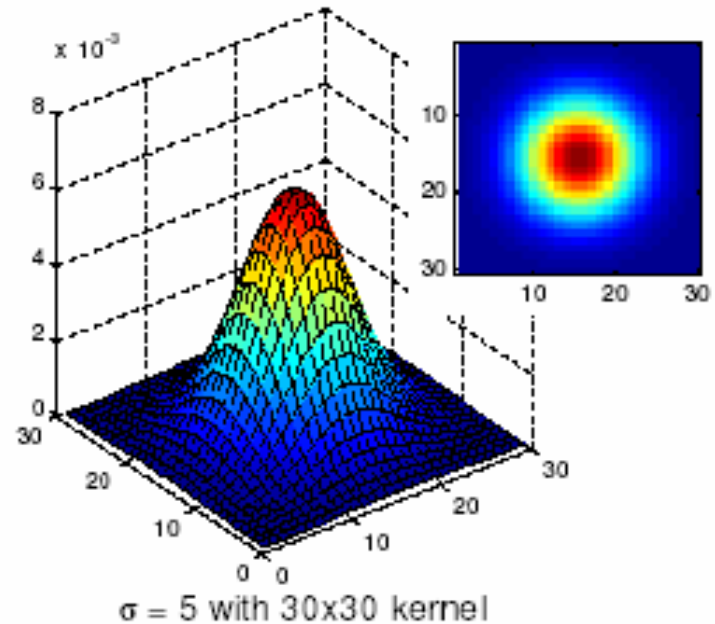
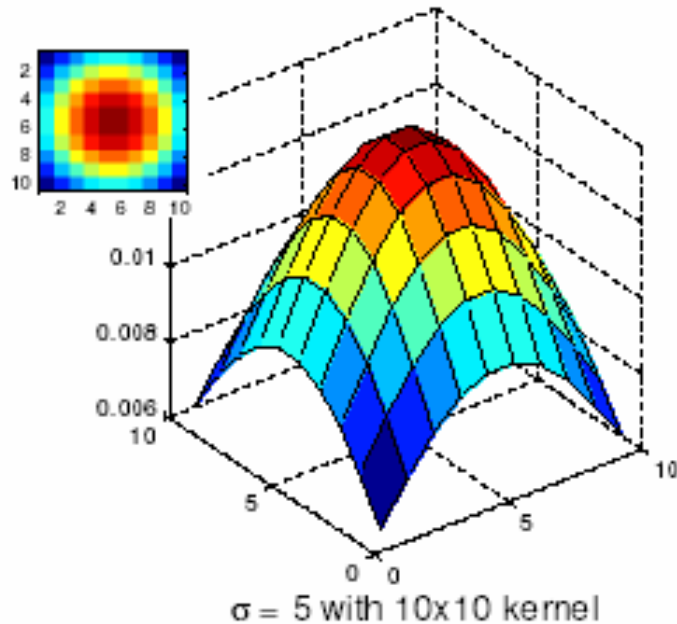
$\sigma = 10$  pixels



$\sigma = 30$  pixels

# Choosing kernel width

- The Gaussian function has infinite support, but discrete filters use finite kernels

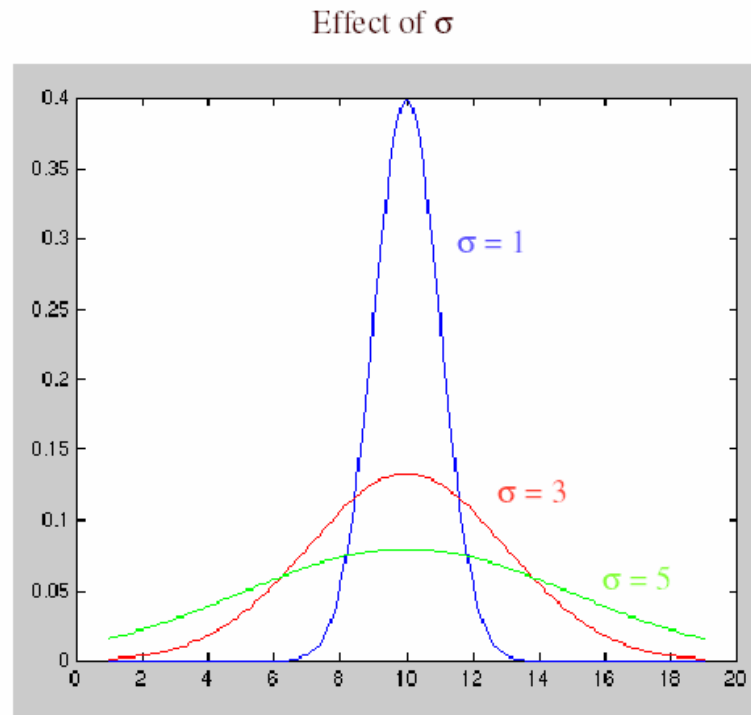


# Practical matters

## How big should the filter be?

Values at edges should be near zero

Rule of thumb for Gaussian: set filter half-width to about  $3\sigma$



# Cross-correlation vs. Convolution

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**cross-correlation:**  $G = H \otimes F$

$$G[i, j] = \sum_{u=-k}^k \sum_{v=-k}^k H[u, v] F[i + u, j + v]$$

A **convolution** operation is a cross-correlation where the filter is flipped both horizontally and vertically before being applied to the image:

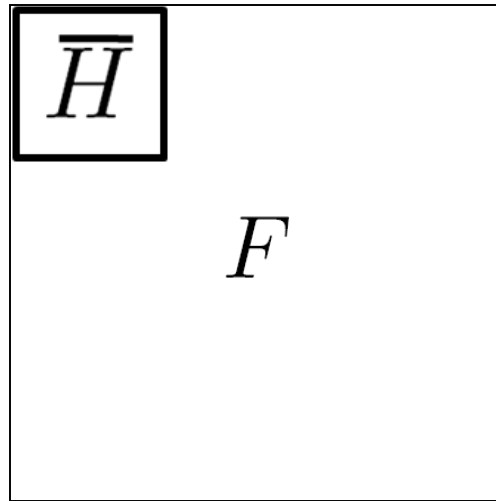
$$G[i, j] = \sum_{u=-k}^k \sum_{v=-k}^k H[u, v] F[i - u, j - v]$$

It is written:

$$G = H \star F$$



# Convolution



# Cross-correlation vs. Convolution

---

**cross-correlation:**  $G = H \otimes F$

$$G[i, j] = \sum_{u=-k}^k \sum_{v=-k}^k H[u, v] F[i + u, j + v]$$

A **convolution** operation is a cross-correlation where the filter is flipped both horizontally and vertically before being applied to the image:

$$G[i, j] = \sum_{u=-k}^k \sum_{v=-k}^k H[u, v] F[i - u, j - v]$$

It is written:

$$G = H \star F$$

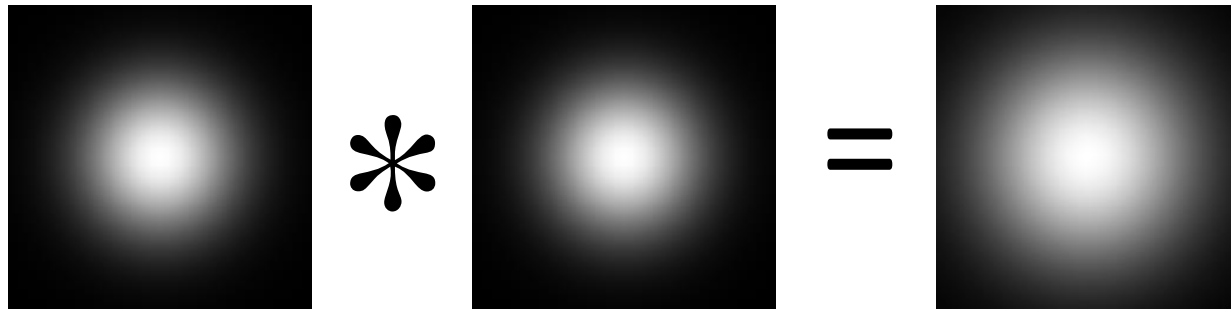
Convolution is **commutative** and **associative**

# Convolution is nice!

- Notation:  $b = c \star a$
- Convolution is a multiplication-like operation
  - commutative  $a \star b = b \star a$
  - associative  $a \star (b \star c) = (a \star b) \star c$
  - distributes over addition  $a \star (b + c) = a \star b + a \star c$
  - scalars factor out  $\alpha a \star b = a \star \alpha b = \alpha(a \star b)$
  - identity: unit impulse  $e = [\dots, 0, 0, 1, 0, 0, \dots]$ 
$$a \star e = a$$
- Conceptually no distinction between filter and signal
- Usefulness of associativity
  - often apply several filters one after another:  $((a \star b_1) \star b_2) \star b_3$
  - this is equivalent to applying one filter:  $a \star (b_1 \star b_2 \star b_3)$

# Gaussian and convolution

- Removes “high-frequency” components from the image (low-pass filter)
- Convolution with self is another Gaussian



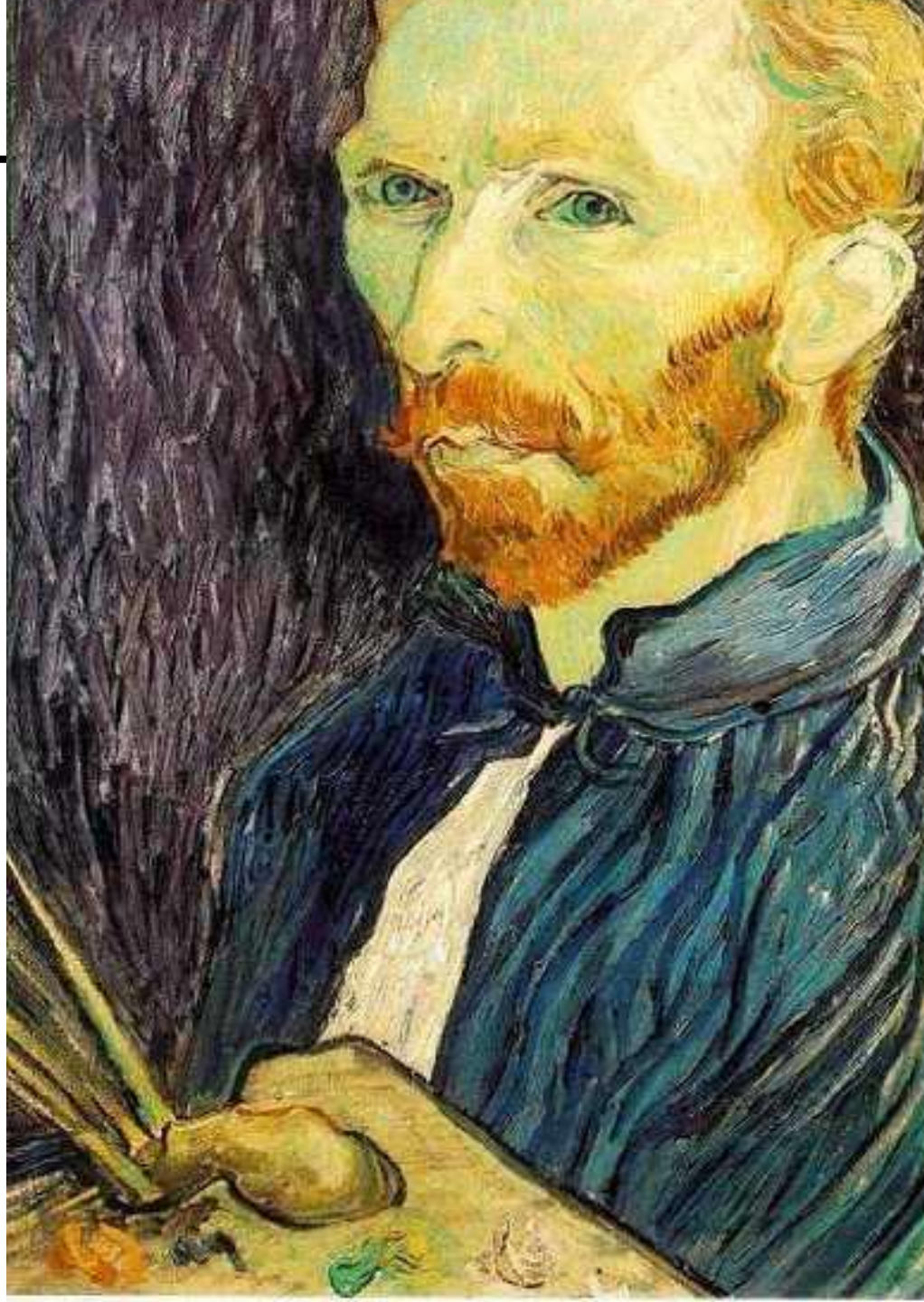
- Convolving twice with Gaussian kernel of width  $\sigma$   
= convolving once with kernel of width  $\sigma\sqrt{2}$

# Image half-sizing

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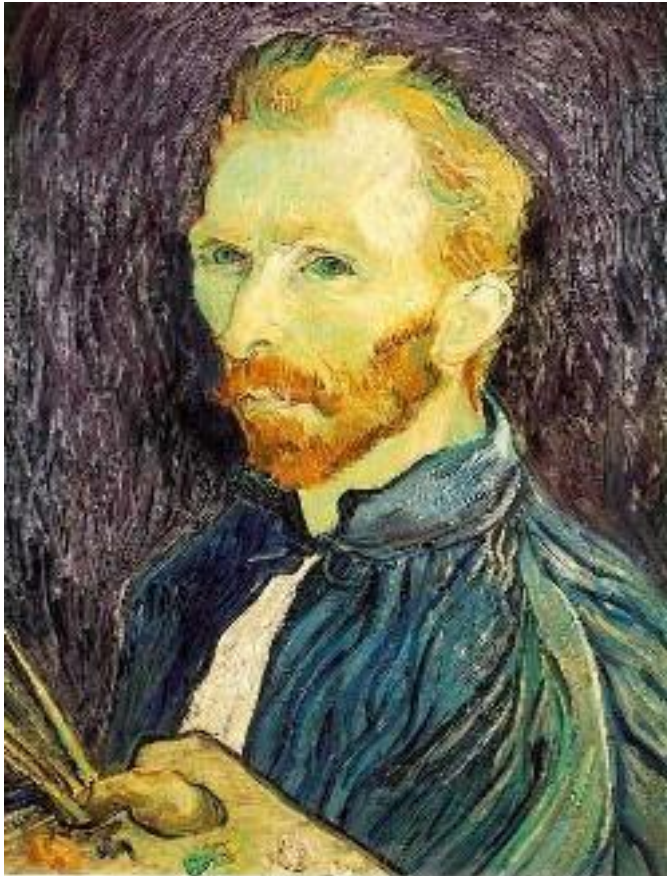
This image is too big to fit on the screen. How can we reduce it?

How to generate a half-sized version?



# Image sub-sampling

---



1/4



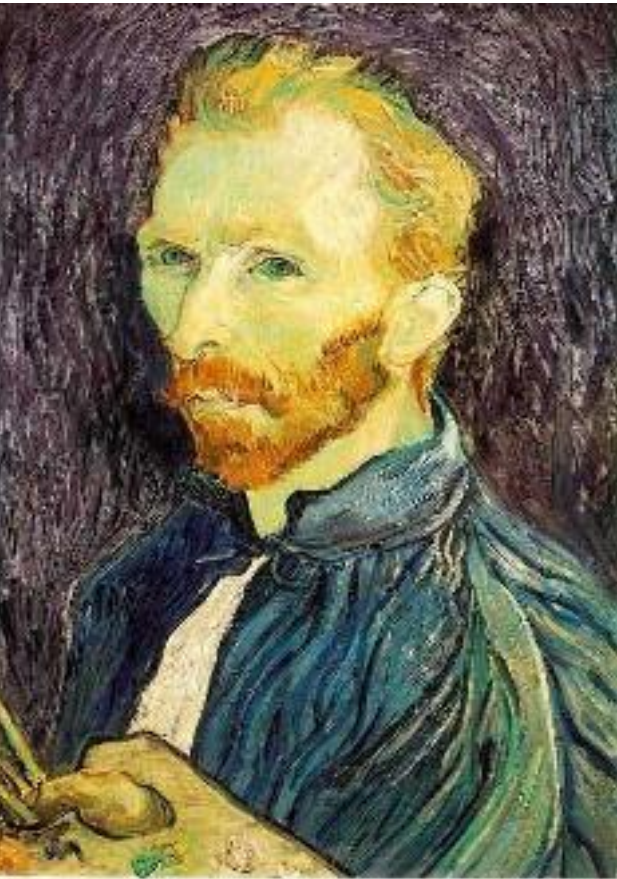
1/8

Throw away every other row and column to create a 1/2 size image  
- called *image sub-sampling*



# Image sub-sampling

---



1/2



1/4 (2x zoom)

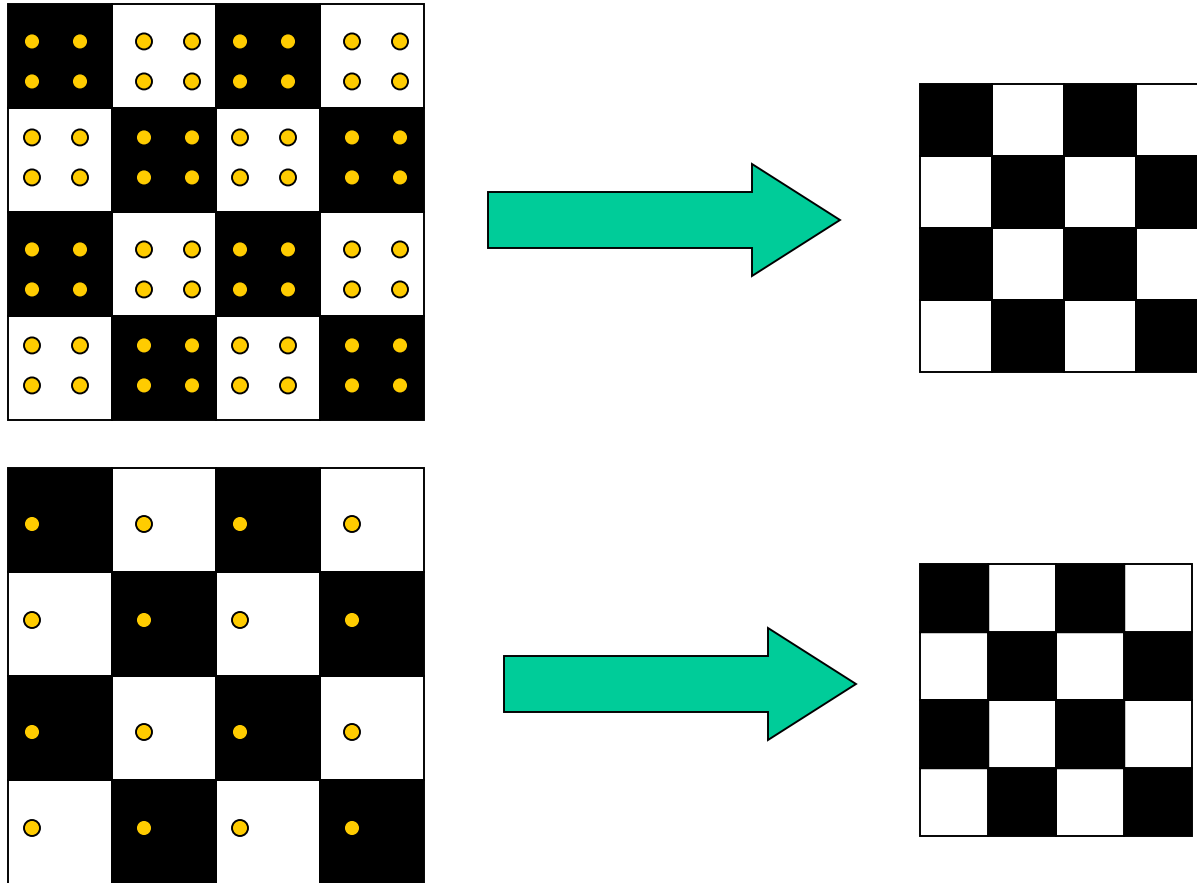


1/8 (4x zoom)

Aliasing! What do we do?

# Sampling an image

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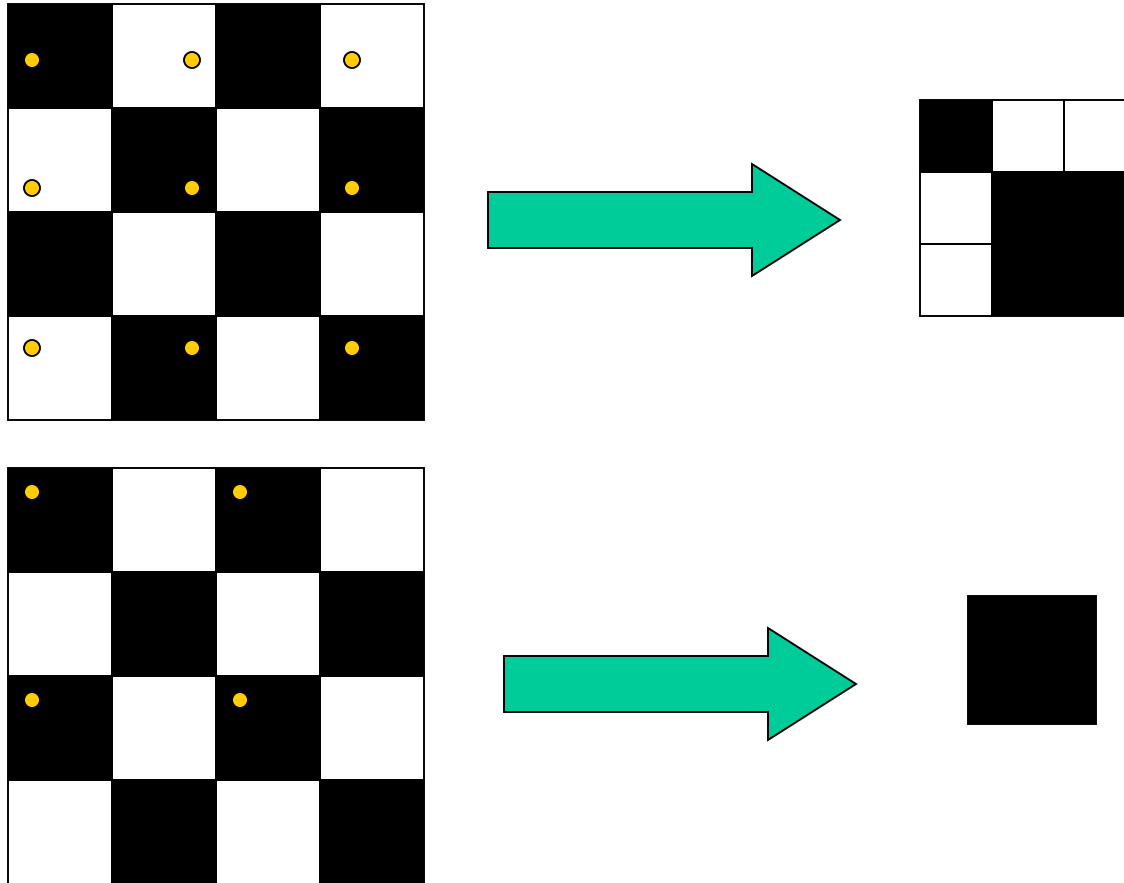


Examples of GOOD sampling



# Undersampling

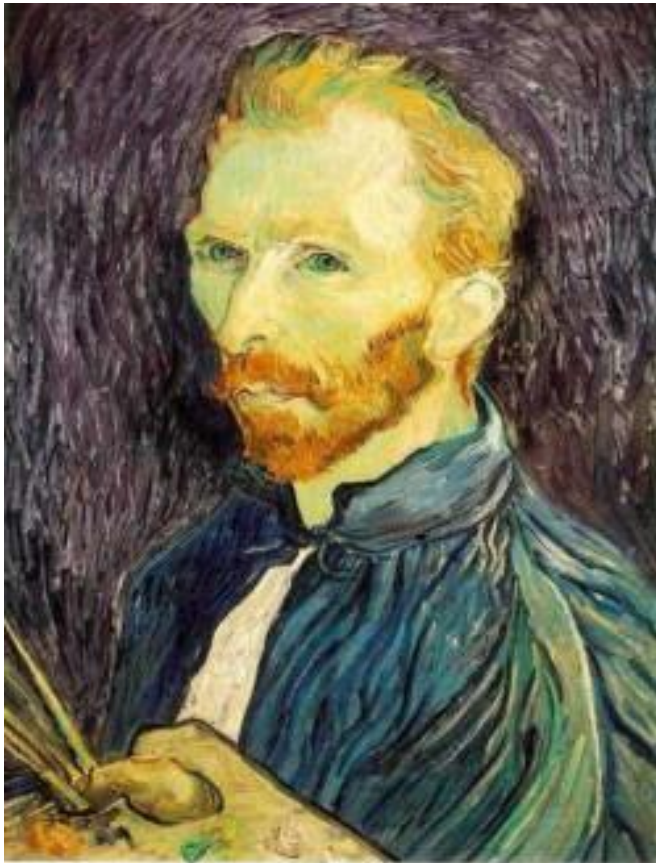
---



Examples of BAD sampling -> Aliasing

# Gaussian (lowpass) pre-filtering

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Gaussian 1/2



G 1/4



G 1/8

Solution: filter the image, *then* subsample

- Filter size should double for each  $\frac{1}{2}$  size reduction. Why?

# Subsampling with Gaussian pre-filtering



Gaussian 1/2



G 1/4

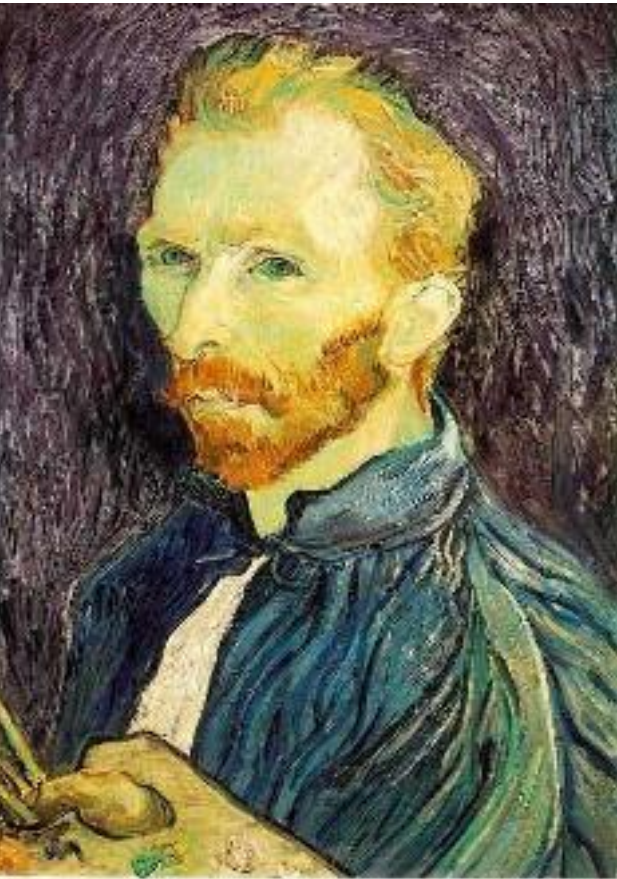


G 1/8



# Compare with...

---



1/2



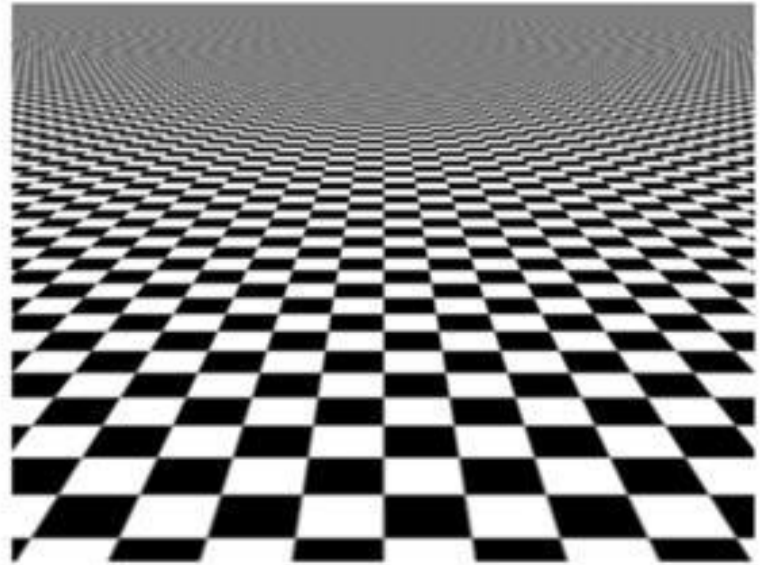
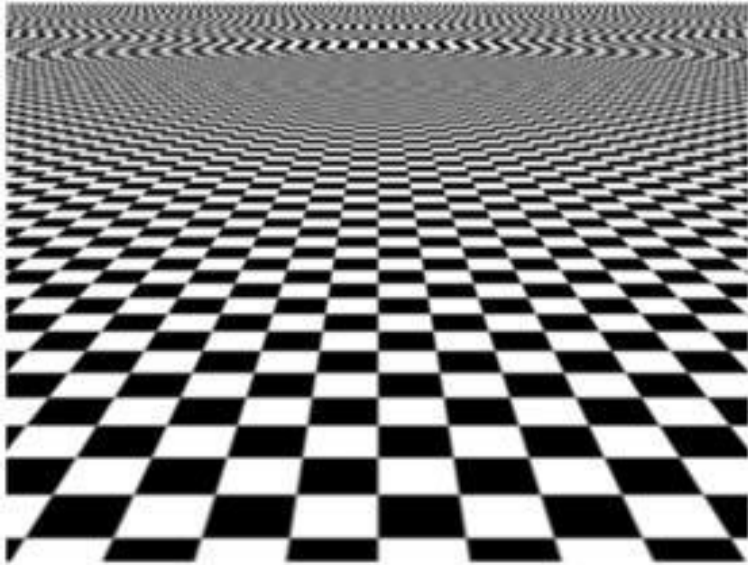
1/4 (2x zoom)



1/8 (4x zoom)

# More Gaussian pre-filtering

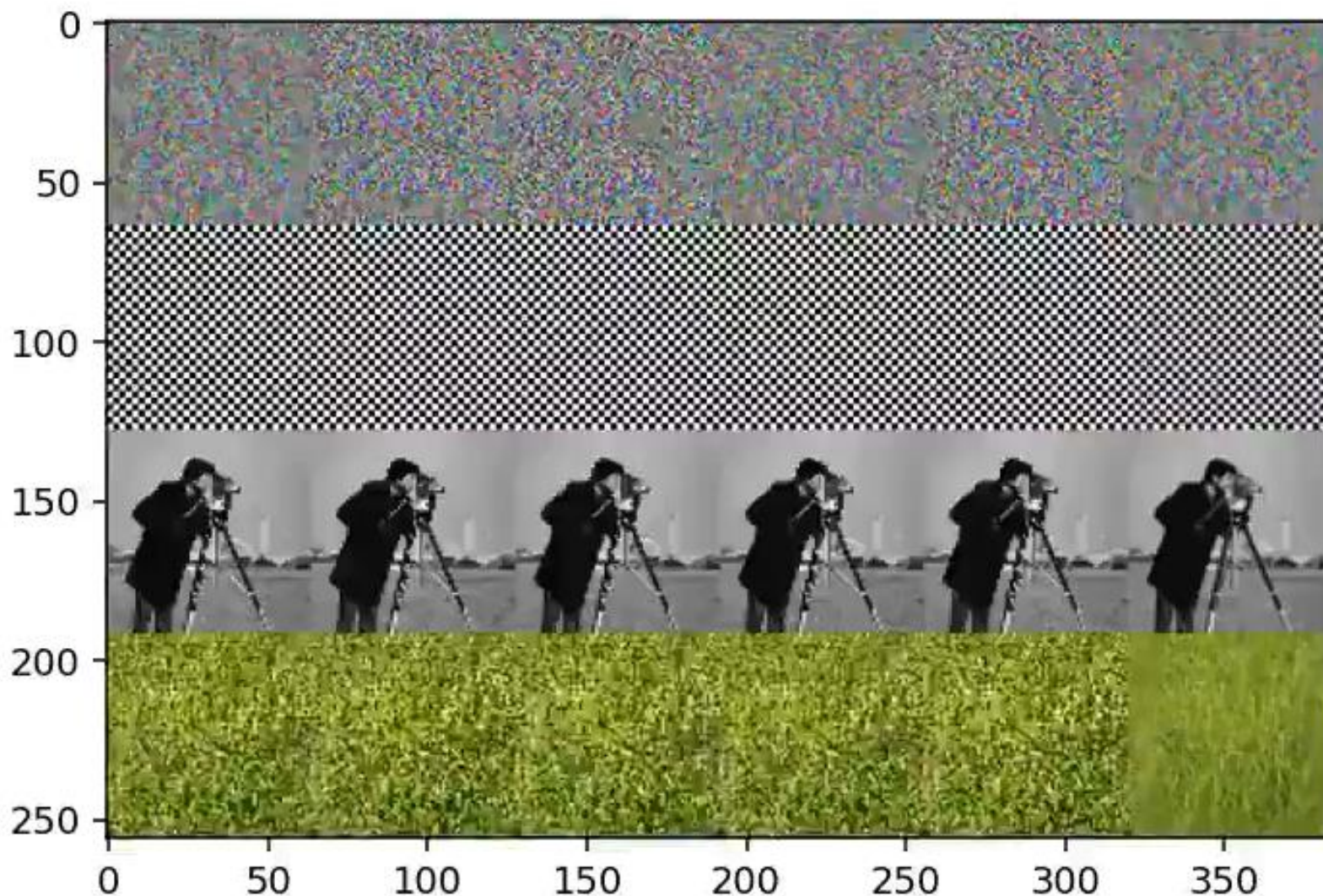
---





# A real problem!

128 x 128  $\rightarrow$  64x64



Open-CV:  
default, bicubic, Lanczos4

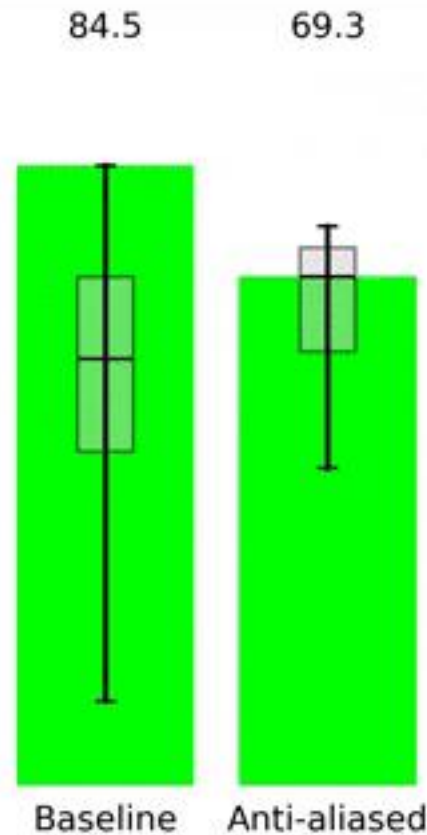
Pytorch:  
bilinear, bicubic

PIL: Lanczos

[Credit: @jaakkolehtinen](#)

# problems in ConvNets too

---

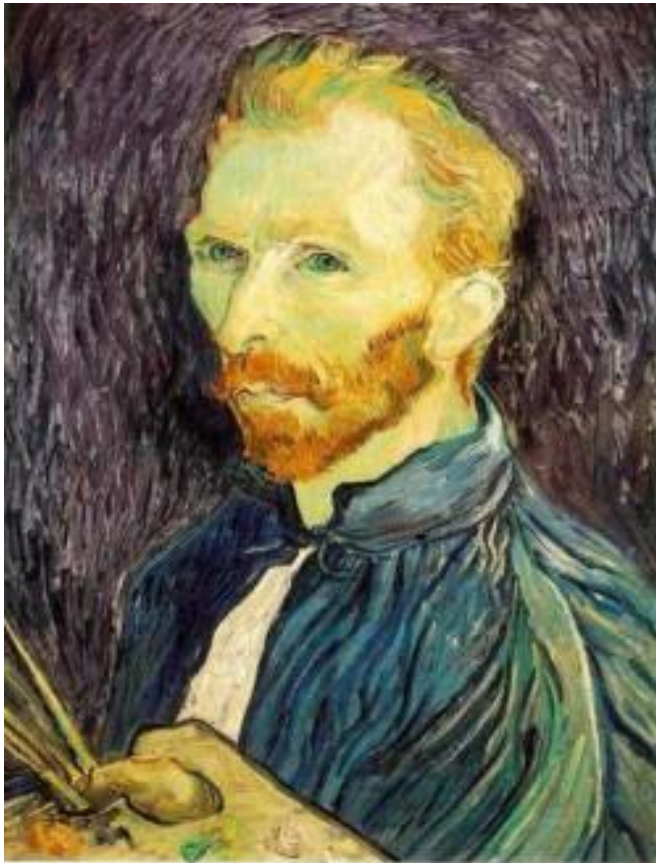


```
pip install antialiased-cnns
```

Making Convolutional Networks Shift-Invariant Again,  
Richard Zhang ICML 2019

# Iterative Gaussian (lowpass) pre-filtering

---



Gaussian  $1/2$



G  $1/4$



G  $1/8$

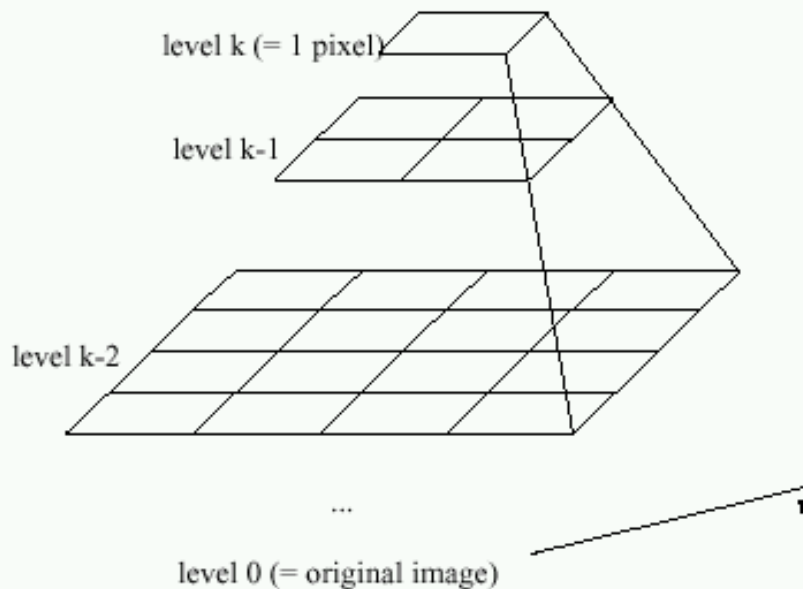
filter the image, *then* subsample

- Filter size should double for each  $\frac{1}{2}$  size reduction. Why?
- How can we speed this up?



# Image Pyramids

Idea: Represent  $N \times N$  image as a “pyramid” of  $1 \times 1, 2 \times 2, 4 \times 4, \dots, 2^k \times 2^k$  images (assuming  $N = 2^k$ )



Known as a **Gaussian Pyramid** [Burt and Adelson, 1983]

- In computer graphics, a *mip map* [Williams, 1983]
- A precursor to *wavelet transform*



512

256

128

64

32

16

8

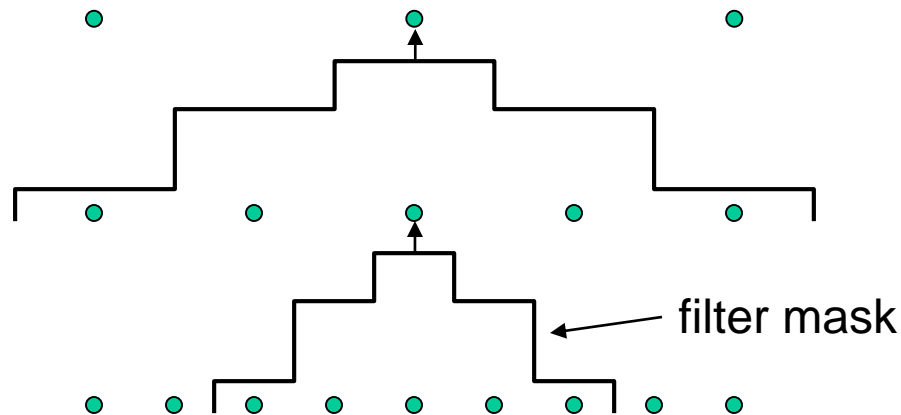
A bar in the big images is a hair on the zebra's nose; in smaller images, a stripe; in the smallest, the animal's nose



The whole pyramid is only  $\frac{4}{3}$  the size of the original image!

# Gaussian pyramid construction

---



Repeat

- Filter
- Subsample

Until minimum resolution reached

- can specify desired number of levels (e.g., 3-level pyramid)

# What are they good for?

---

## Improve Search

- Search over translations
  - Classic coarse-to-fine strategy
  - Project 1!
- Search over scale
  - Template matching
  - E.g. find a face at different scales

# What else are convolutions good for?

---

Taking derivative by convolution  
(on board)

# Partial derivatives with convolution

---

Image is function  $f(x,y)$

Remember:

$$\frac{\partial f(x, y)}{\partial x} = \lim_{\epsilon \rightarrow 0} \frac{f(x + \epsilon, y) - f(x, y)}{\epsilon}$$

Approximate:

-1	1
----	---

$$\frac{\partial f(x, y)}{\partial x} \approx \frac{f(x + 1, y) - f(x, y)}{1}$$

Another one:

-1	0	1
----	---	---

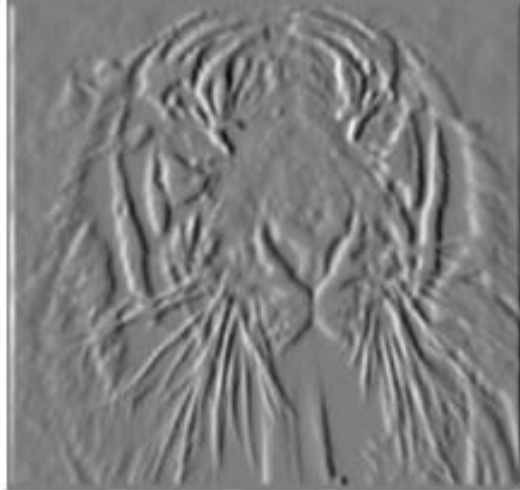
$$\frac{\partial f(x, y)}{\partial x} \approx \frac{f(x + 1, y) - f(x - 1, y)}{2}$$

# Partial derivatives of an image

---

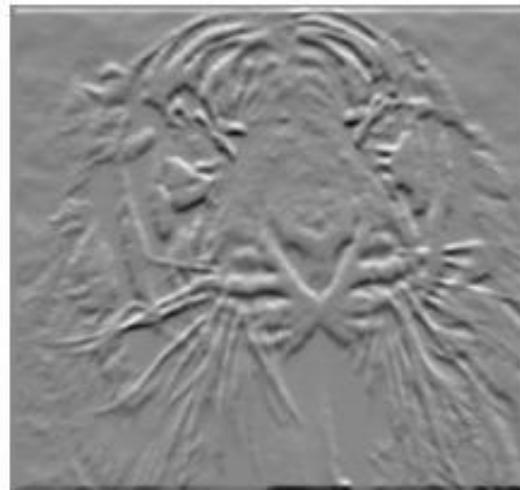


$$\frac{\partial f(x, y)}{\partial x}$$



-1	1
----	---

$$\frac{\partial f(x, y)}{\partial y}$$



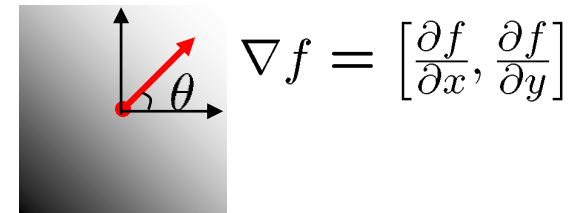
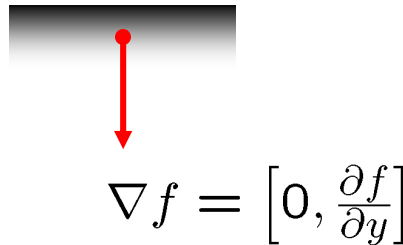
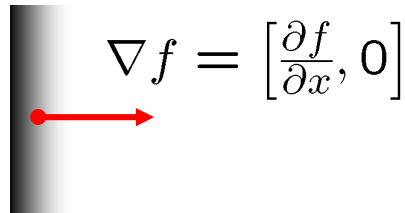
-1	or	1
1		-1

Which shows changes with respect to x?

# Image gradient

---

The gradient of an image:  $\nabla f = \left[ \frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right]$



The gradient points in the direction of most rapid increase in intensity

- How does this direction relate to the direction of the edge?

The *edge strength* is given by the gradient magnitude

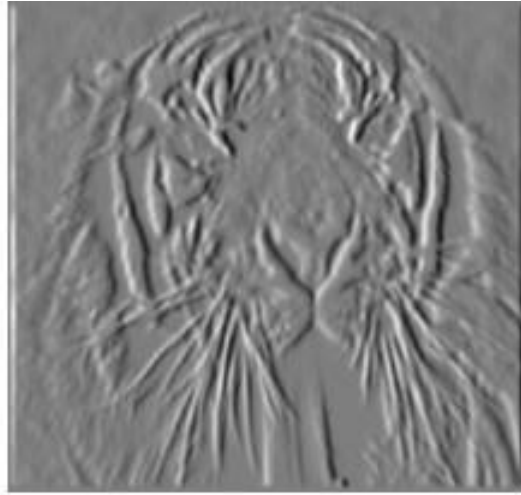
$$\|\nabla f\| = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$

The gradient direction is given by  $\theta = \tan^{-1} \left( \frac{\partial f}{\partial y} / \frac{\partial f}{\partial x} \right)$

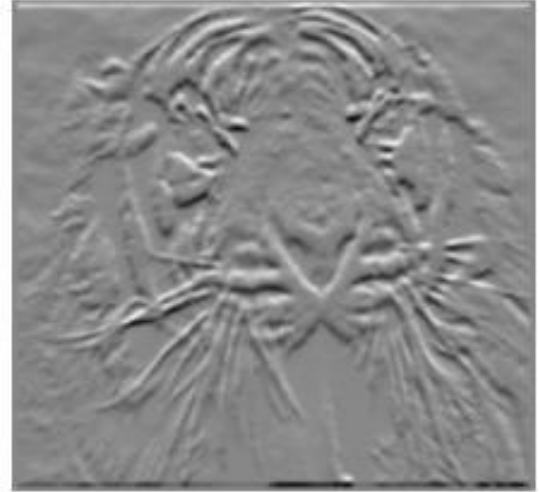


# Image Gradient

---



$$\frac{\partial f(x, y)}{\partial x}$$



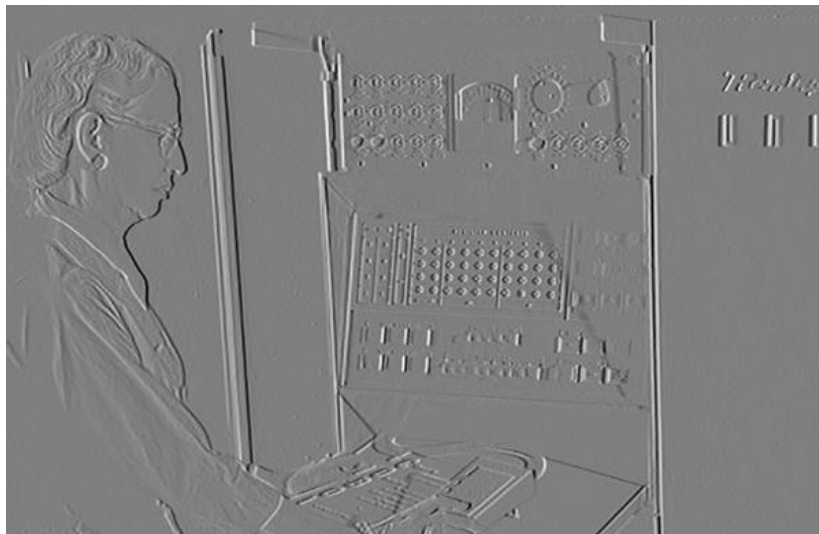
$$\frac{\partial f(x, y)}{\partial y}$$

$$\|\nabla f\| = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$

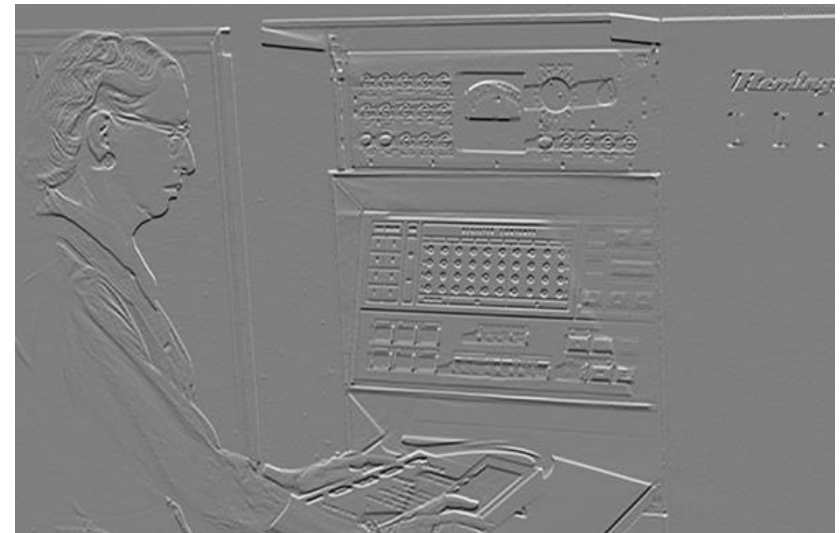


# Partial Derivatives

---



$$\frac{\partial f(x, y)}{\partial x}$$



$$\frac{\partial f(x, y)}{\partial y}$$

# Gradient magnitude

---

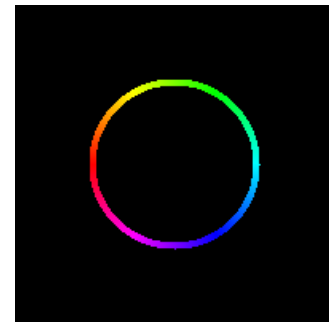
$$\|\nabla f\| = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$



# Gradient Orientation

---

$$\theta = \tan^{-1} \left( \frac{\partial f / \partial y}{\partial f / \partial x} \right) \quad \text{atan2} (dy, dx)$$



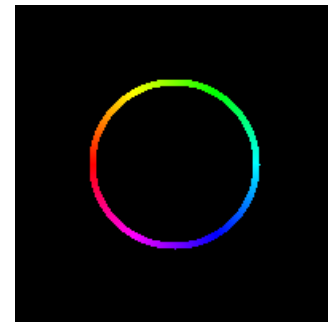
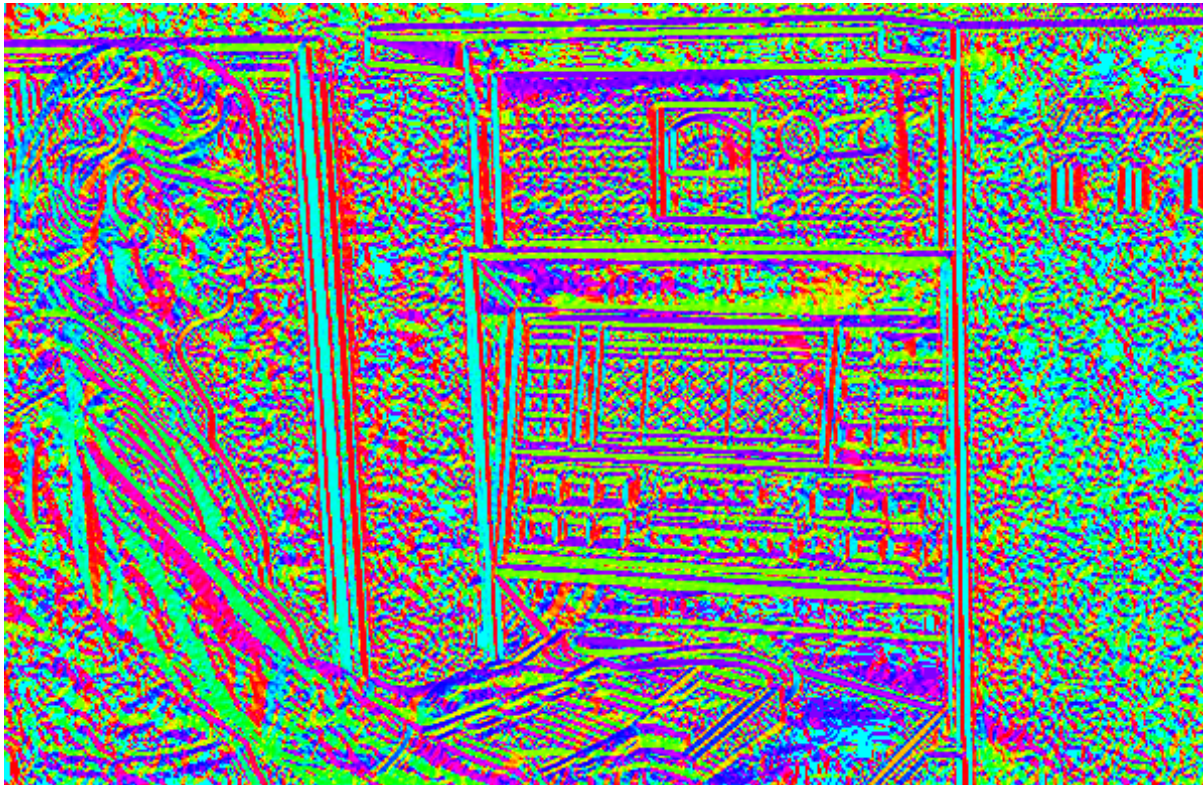
lightness is equal to gradient magnitude



# Image Gradient

---

$$\theta = \tan^{-1} \left( \frac{\partial f}{\partial y} / \frac{\partial f}{\partial x} \right)$$

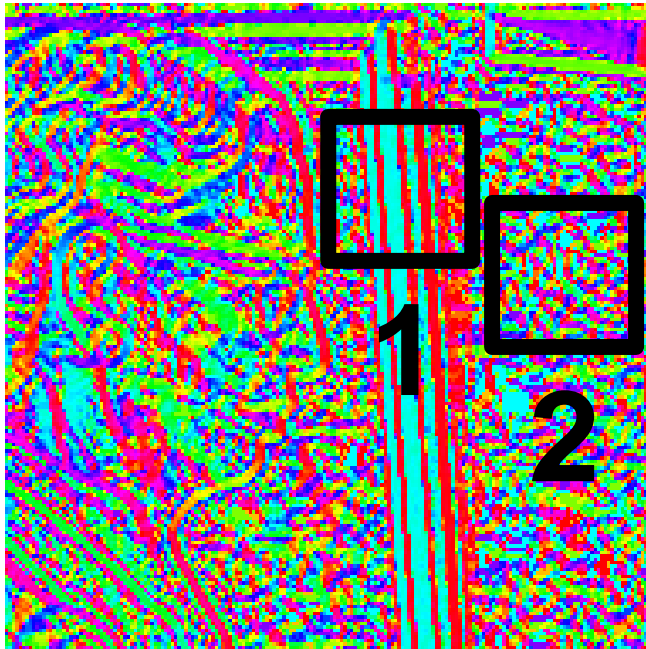


*all the gradients*

# Image Gradient

---

Why is there structure at 1 and not at 2?

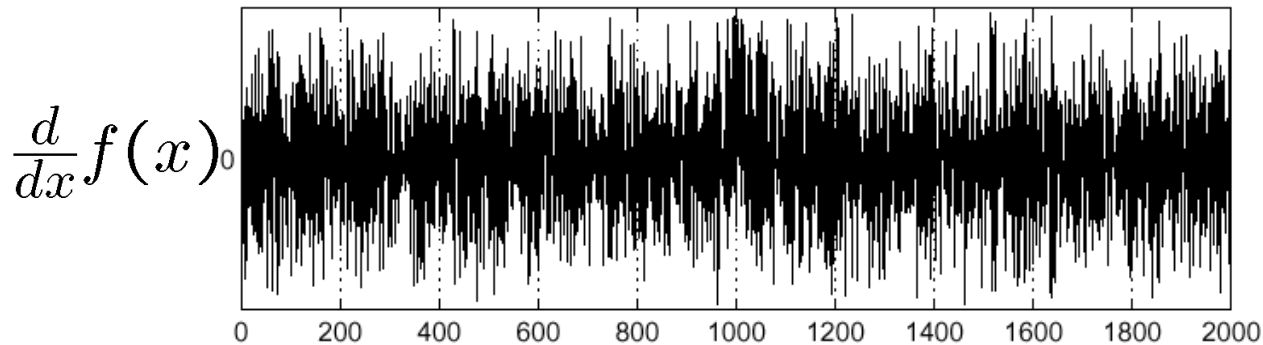
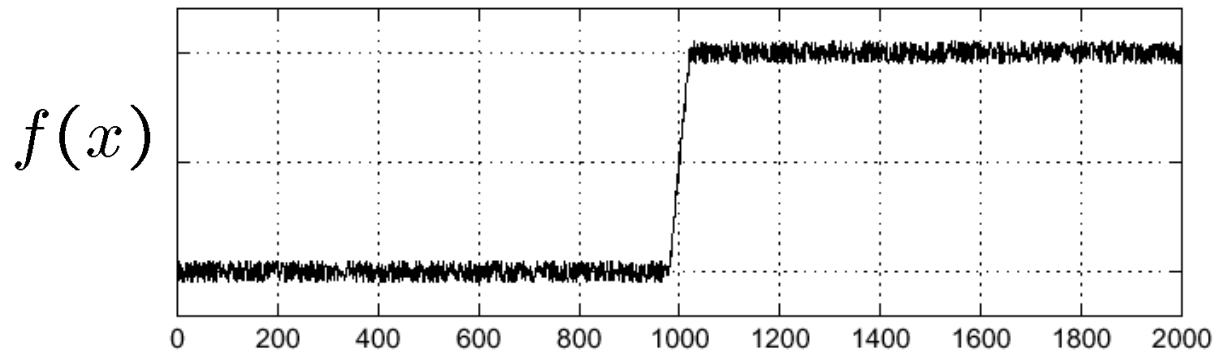


# Effects of noise

---

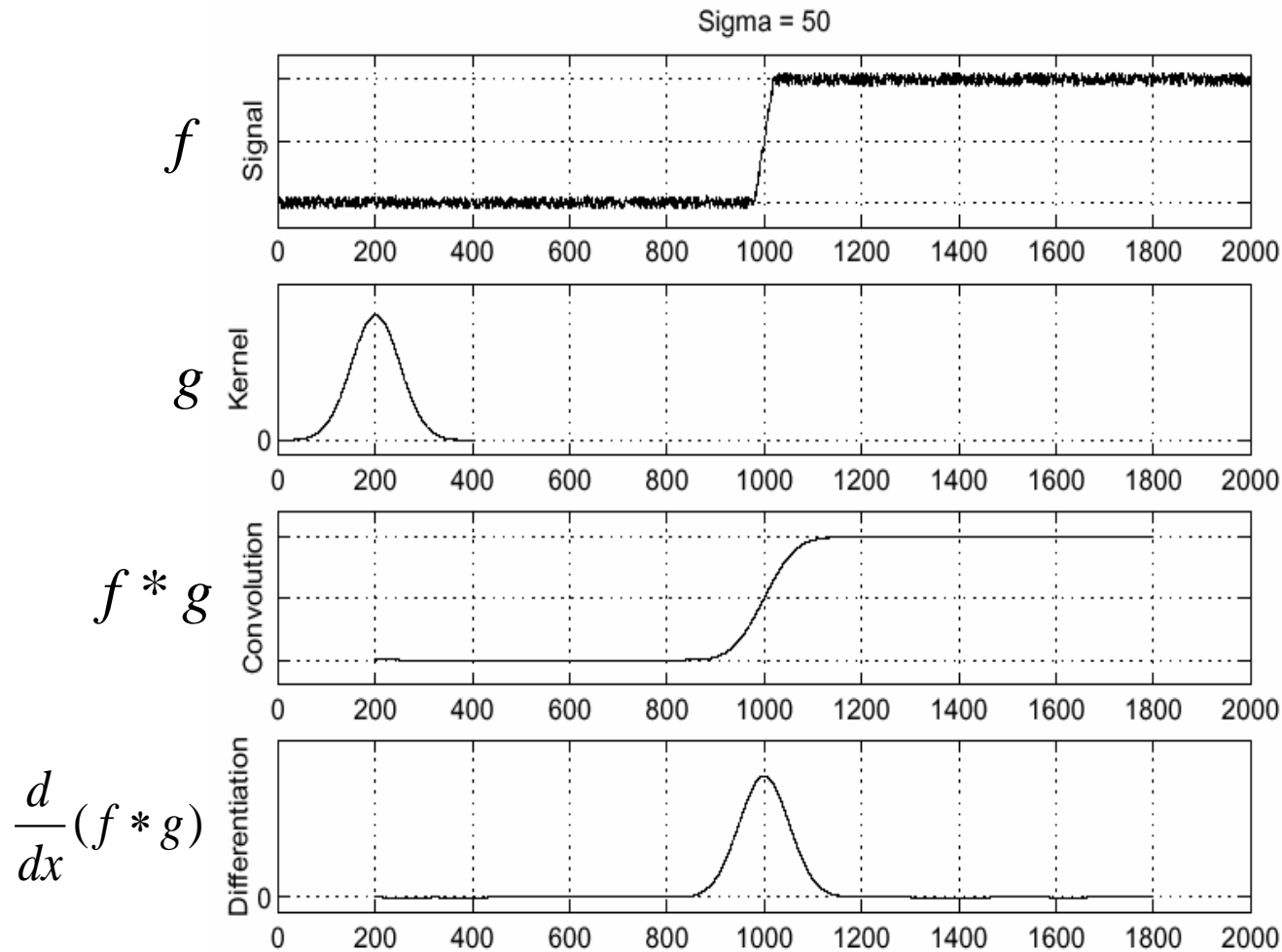
Consider a single row or column of the image

- Plotting intensity as a function of position gives a signal



Where is the edge?

# Solution: smooth first



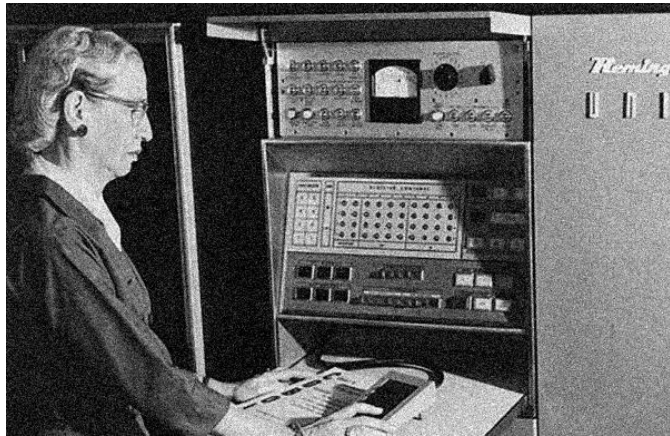
- To find edges, look for peaks in  $\frac{d}{dx}(f * g)$



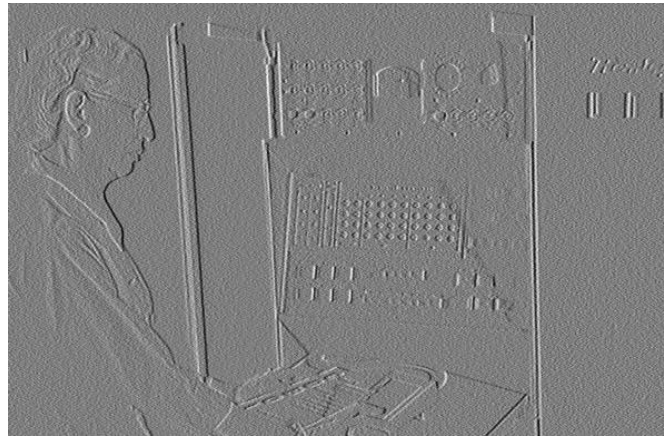
# Noise in 2D

---

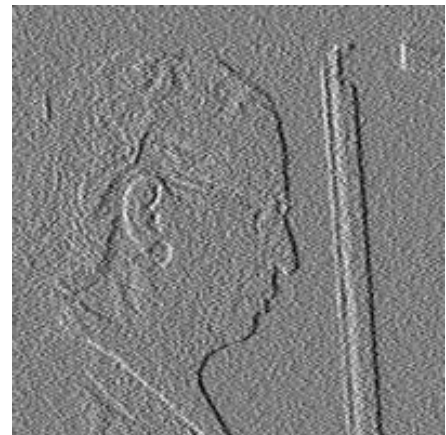
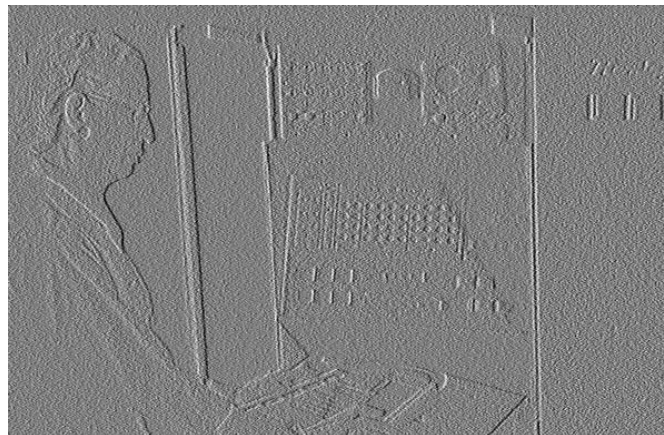
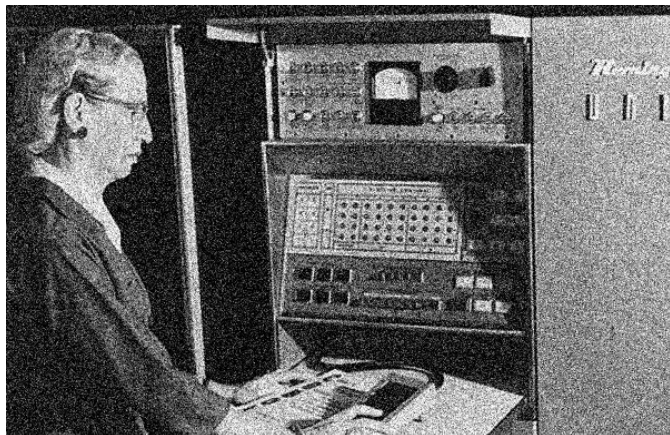
Noisy Input



$dx$  via  $[-1, 01]$



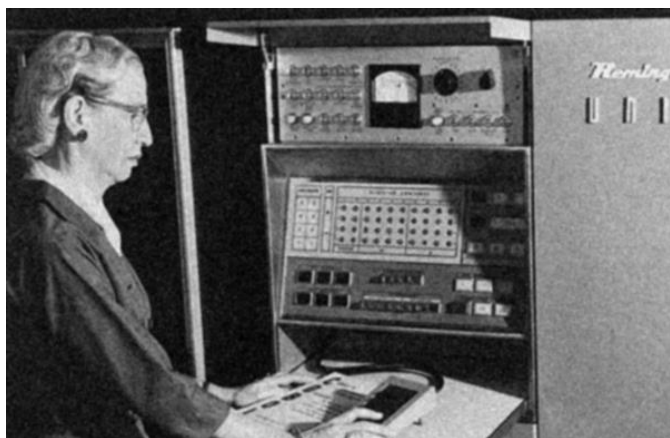
Zoom



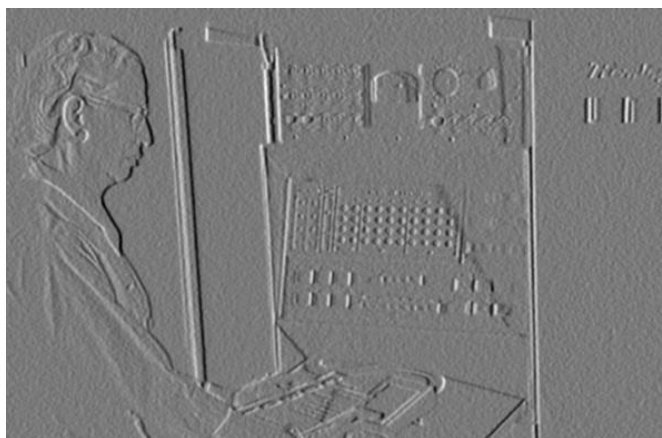
# Noise + Smoothing

---

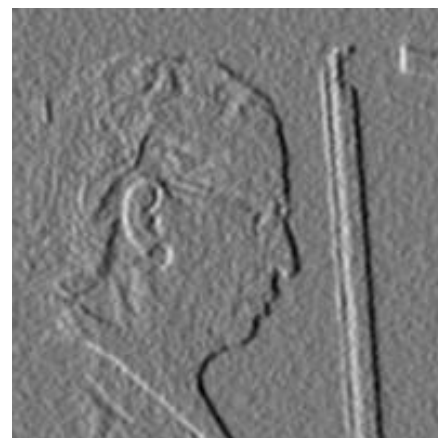
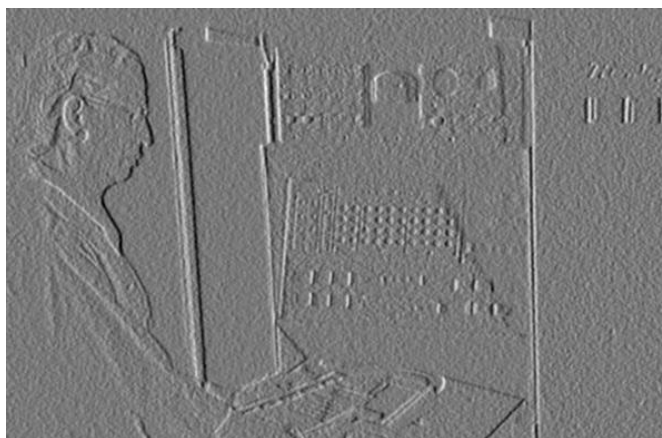
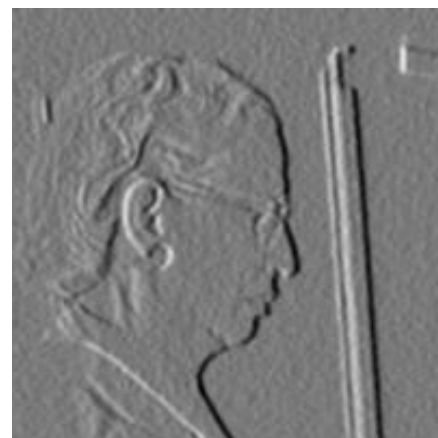
Smoothed Input



$dx$  via  $[-1,0,1]$

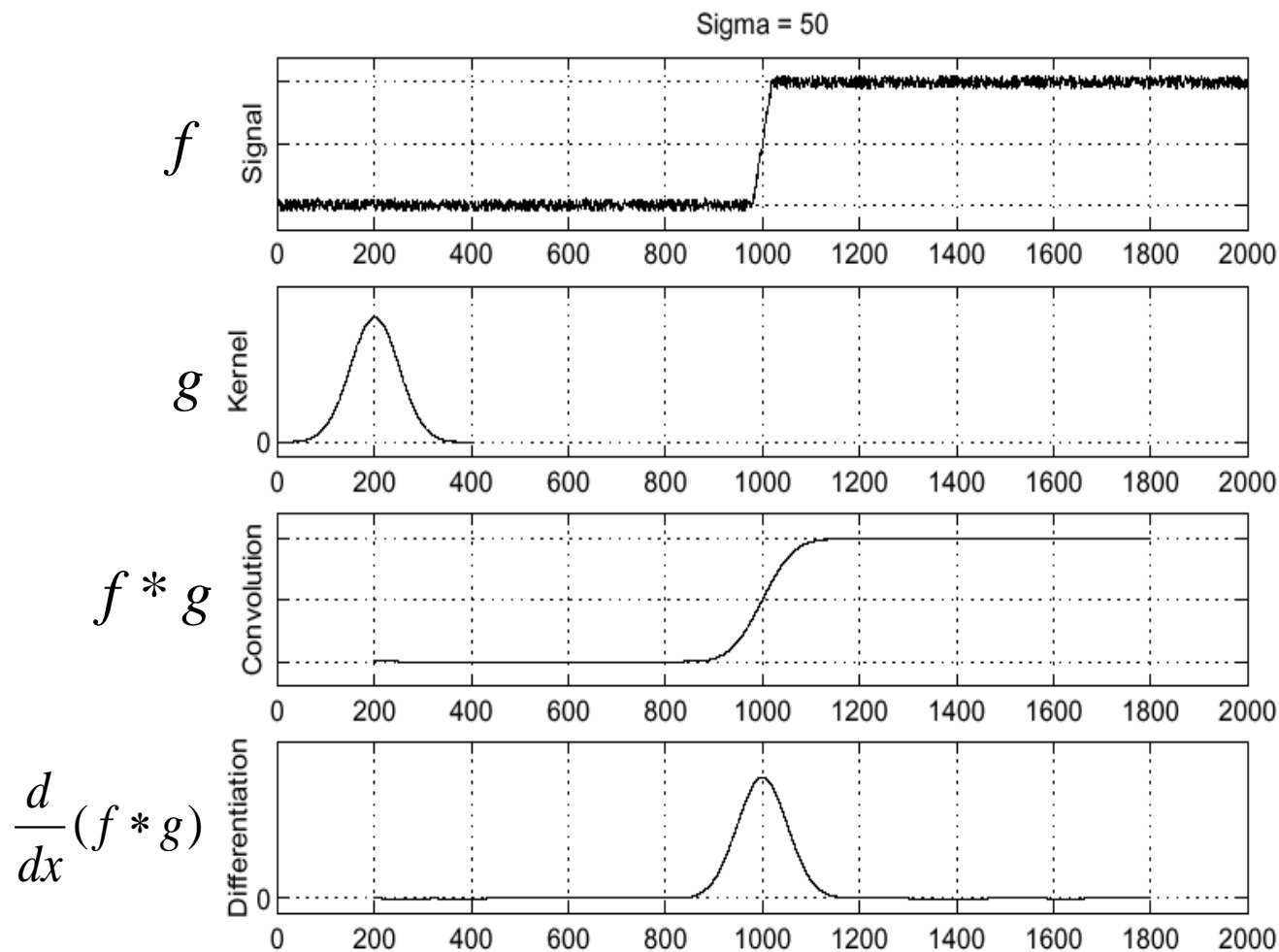


Zoom



# How many convolutions here?

---



can we reduce this?

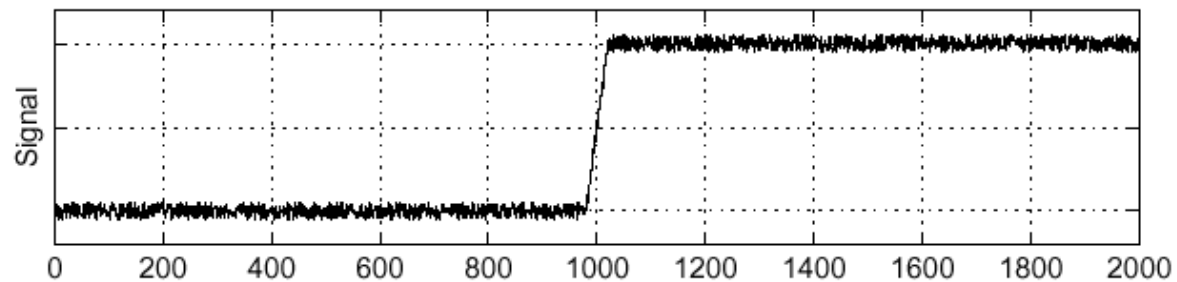
# Derivative theorem of convolution

---

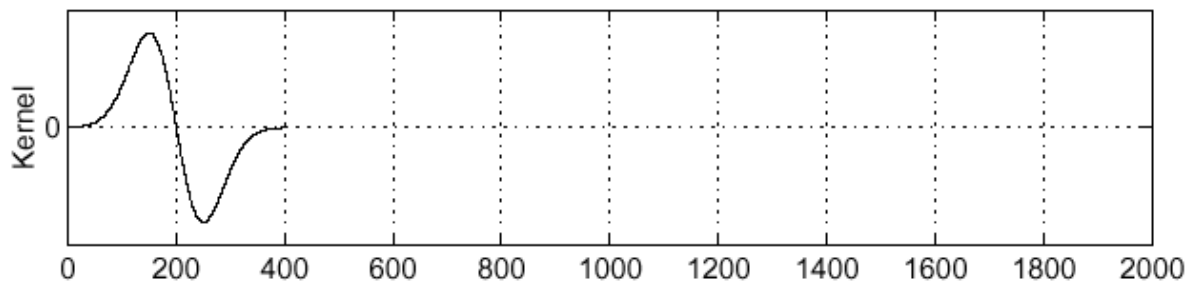
$$\frac{\partial}{\partial x}(h \star f) = \left(\frac{\partial}{\partial x}h\right) \star f$$

This saves us one operation:

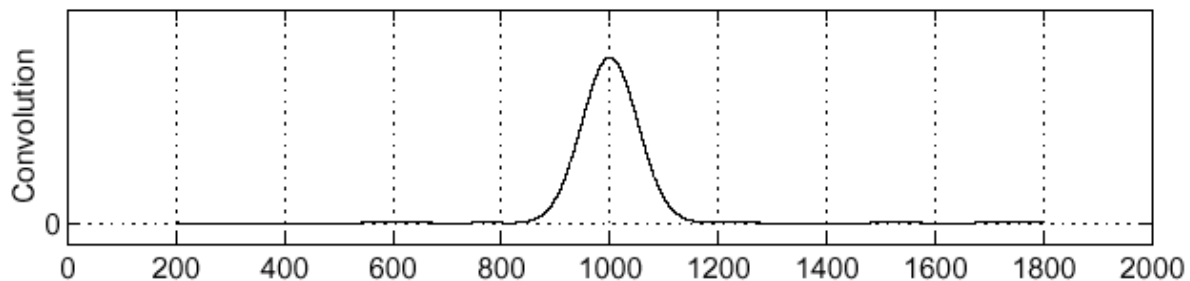
Sigma = 50



$$\frac{\partial}{\partial x}h$$

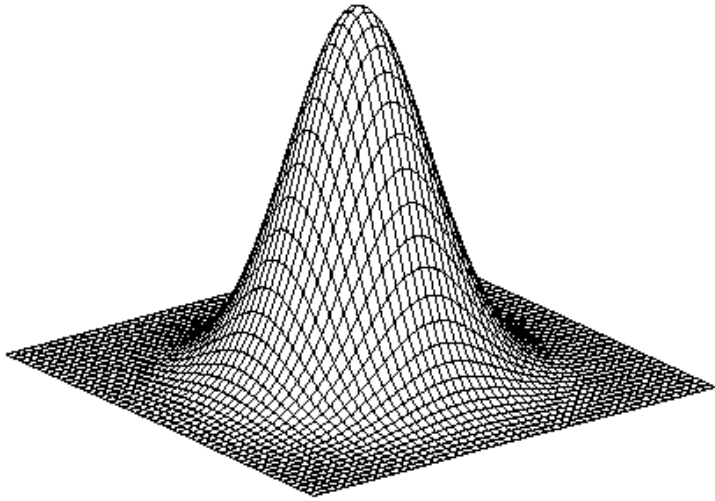


$$\left(\frac{\partial}{\partial x}h\right) \star f$$

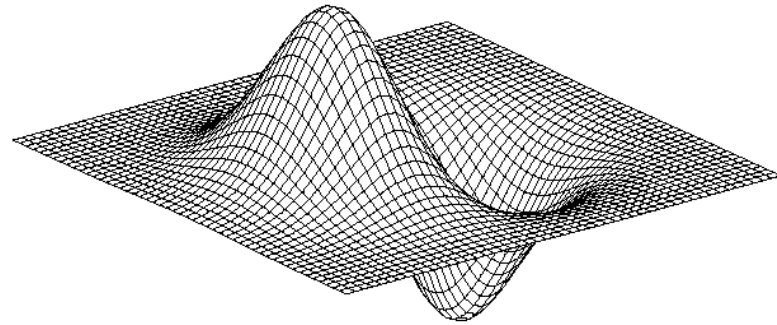


# Derivative of Gaussian filter

---

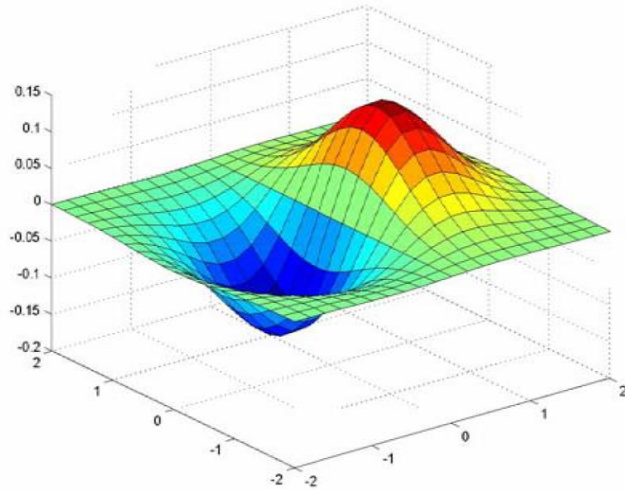


$$* [1 \ 0 \ -1] =$$

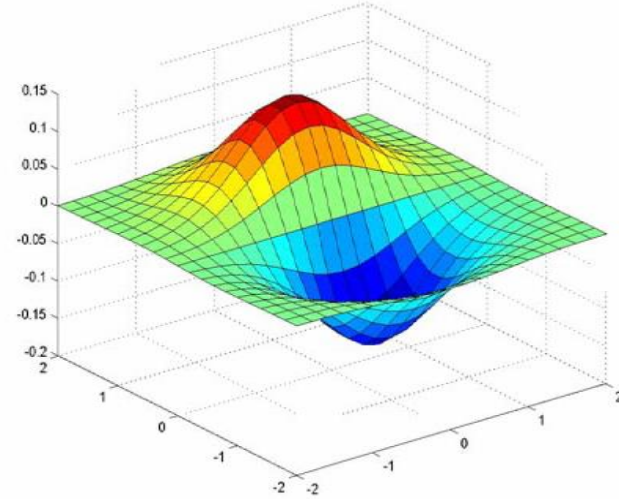
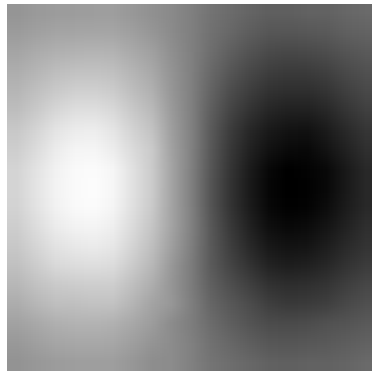


# Derivative of Gaussian filter

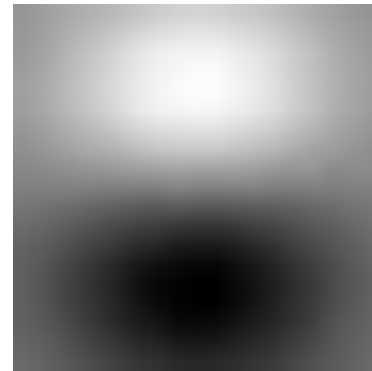
---



x-direction



y-direction



Which one finds horizontal/vertical edges?

# Compare to classic derivative filters

---

**Prewitt:**  $M_x =$ 

-1	0	1
-1	0	1
-1	0	1

 ;  $M_y =$ 

1	1	1
0	0	0
-1	-1	-1

**Sobel:**  $M_x =$ 

-1	0	1
-2	0	2
-1	0	1

 ;  $M_y =$ 

1	2	1
0	0	0
-1	-2	-1

**Roberts:**  $M_x =$ 

0	1
-1	0

 ;  $M_y =$ 

1	0
0	-1

# Low Pass vs. High Pass filtering

---

Image

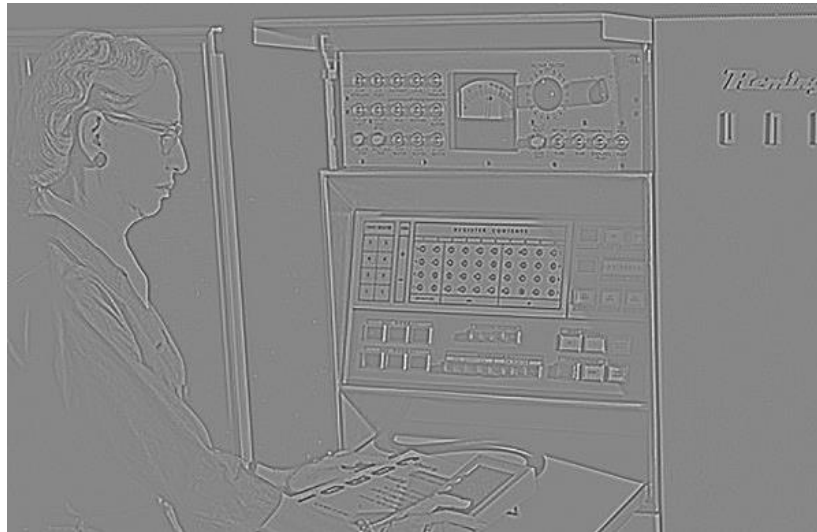


Smoothed



Details

=





# Filtering – Sharpening

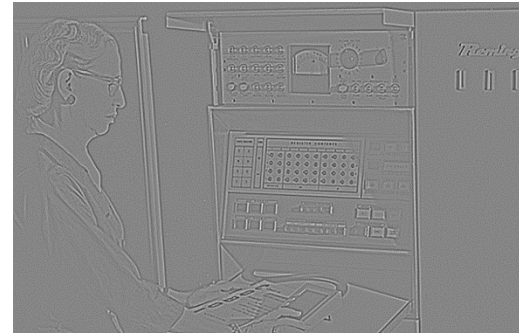
---

Image



$+\alpha$

Details



“Sharpened”  $\alpha=1$

$=$



# Filtering – Sharpening

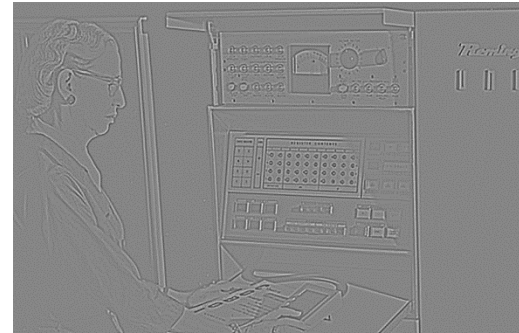
---

Image



$+\alpha$

Details



“Sharpened”  $\alpha=0$

$=$



# Filtering – Sharpening

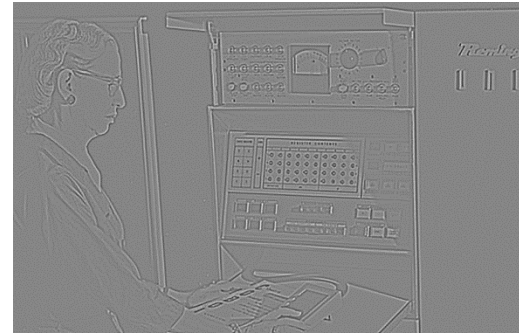
---

Image



$+\alpha$

Details



“Sharpened”  $\alpha=2$

$=$



# Filtering – Sharpening

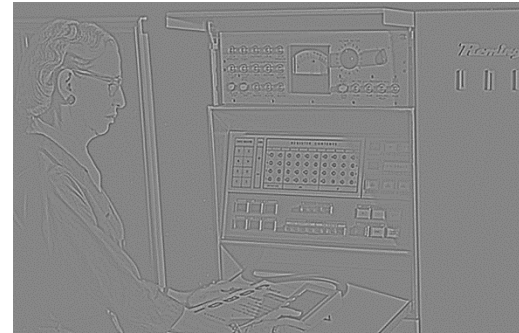
---

Image



$+\alpha$

Details



“Sharpened”  $\alpha=0$

=



# Filtering – Extreme Sharpening

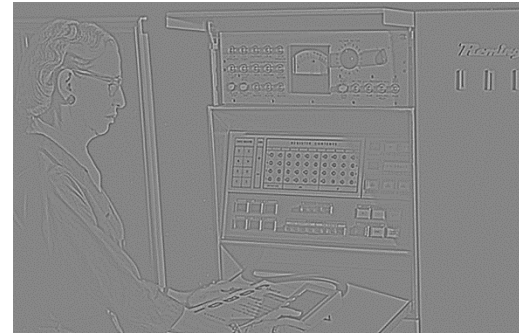
---

Image



$+\alpha$

Details



“Sharpened”  $\alpha=10$

$=$



# Unsharp mask filter (= sharpening filter)

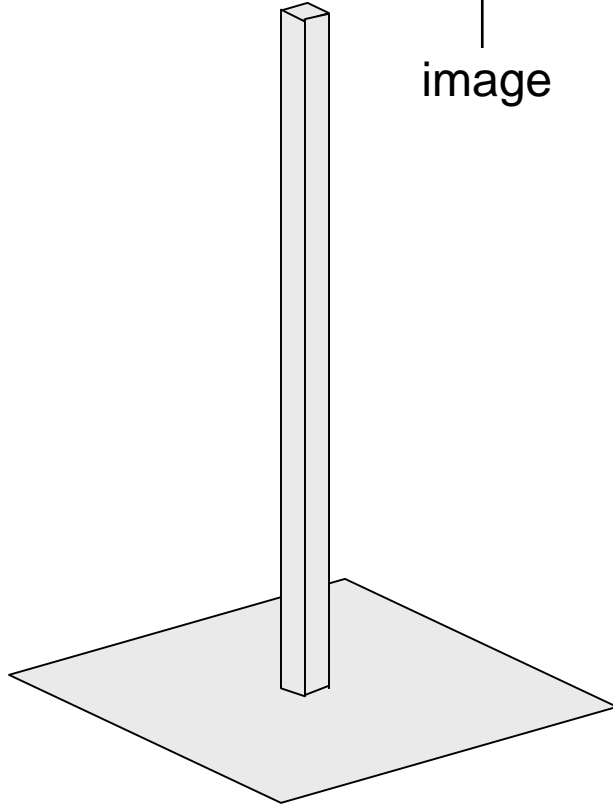
---

$$f + \alpha(f - f * g) = (1 + \alpha)f - \alpha f * g = f * ((1 + \alpha)e - \alpha g)$$

↑  
image

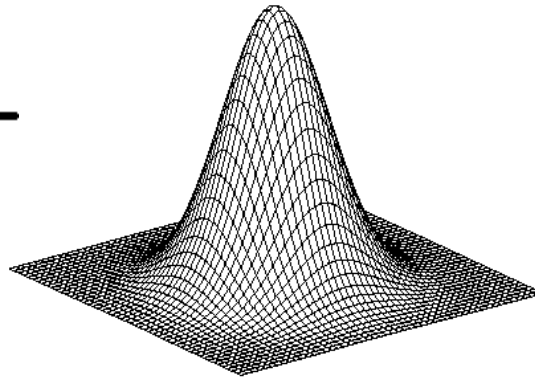
↑  
blurred  
image

↑  
unit impulse  
(identity)



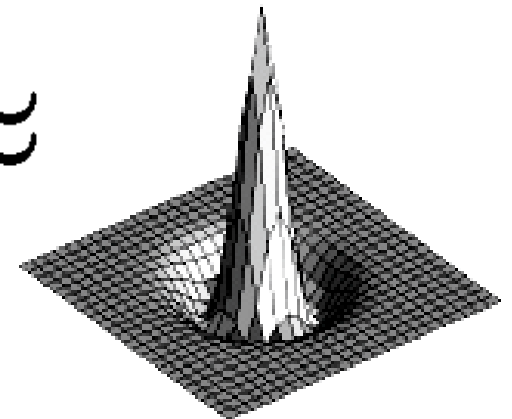
unit impulse

—



Gaussian

≈



Laplacian of Gaussian

# Filtering: practical matters

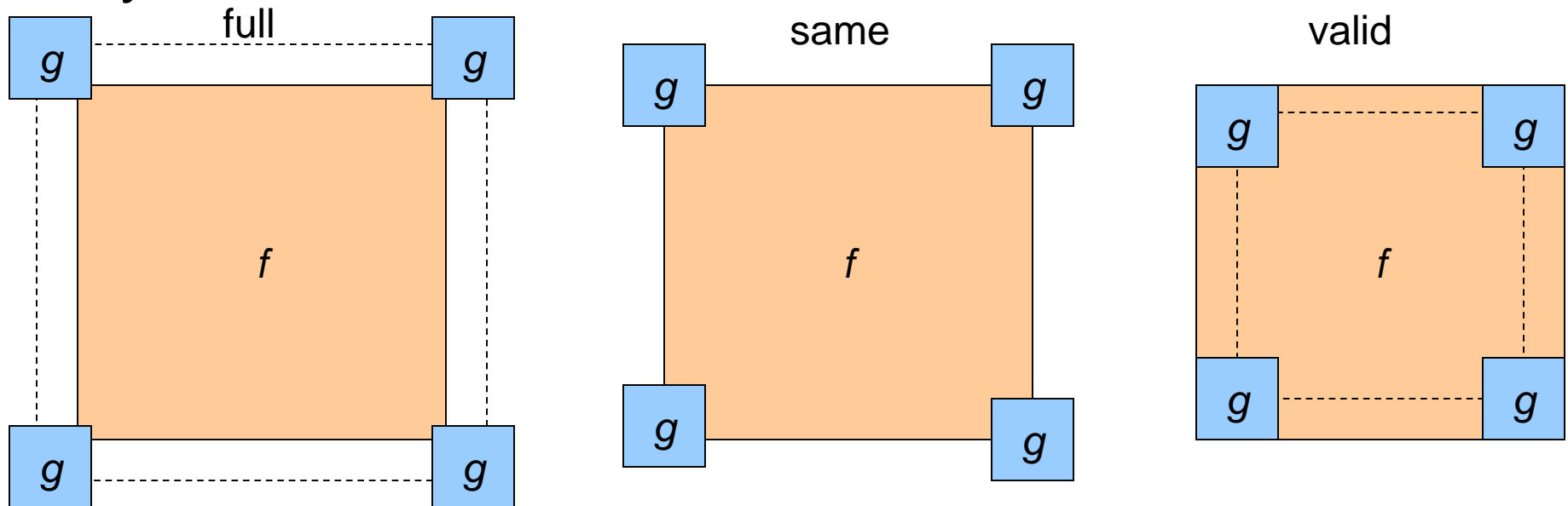
---

What is the size of the output?

(MATLAB) `filter2(g, f, shape)` or `conv2(g,f,shape)`

- *shape* = 'full': output size is sum of sizes of *f* and *g*
- *shape* = 'same': output size is same as *f*
- *shape* = 'valid': output size is difference of sizes of *f* and *g*

Pytorch `conv2d` 'valid' or 'same'



# Practical matters

---

## What about near the edge?

- the filter window falls off the edge of the image
- need to extrapolate
- methods:
  - clip filter (black)
  - wrap around (circular)
  - copy edge
  - reflect across edge

