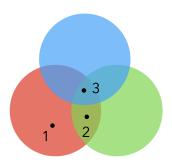
# **NeRF** Fundamentals

Discussion #9

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## 1 Alpha Compositing

Suppose we're trying to overlay 3 colored R G B circles with translucent opacity on a white background. The formula for overlaying (compositing) color  $c_a$  with opacity (alpha)  $\alpha_a$  over an opaque  $c_b$  is:  $c_{new} = c_a \cdot \alpha_a + c_b \cdot (1 - \alpha_a)$ .



1.1: Enhance! Expand the alpha compositing formula to express the output pixel values at points 1, 2, and 3. Don't forget the background! Also don't worry about simplifying, just expand.

1.2: Simplifying Write your answer for point 3 with 4 terms for r, g, b, and white.

$$C_3 = \alpha_b \cdot C_b + \underline{\qquad} \alpha_g \cdot C_g + \underline{\qquad} \alpha_r \cdot C_r + \underline{\qquad} C_w$$

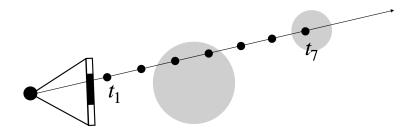
**1.3: Transmittance!** How does the form of this compositing formula look similar to transmittance from a NeRF?  $T(n) = \prod_{k=1}^{n-1} (1 - \alpha_k)$ .

#### Flatland NeRF

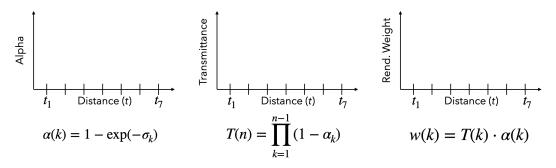
In this sheet, we consider a simplified NeRF in a flat plane. In this setup, 1) Each camera has a 1D sensor array which measures color. 2) All poses and rays exist only in 2 dimensions. 3) The background is known to be white. 4) Only output color c and density  $\sigma$  per-point (we ignore view direction).

### 2 Volume Rendering

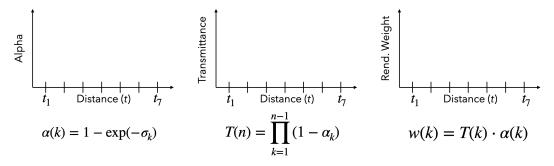
Density in NeRF represents where geometry lies in a scene. During NeRF rendering there are three quantities we derive from density to render color from a ray: **alpha** (opacity), **transmittance**, and **rendering weights**. For simplification, the equations below *omit ray sample spacing*  $\delta_k$  as it is constant.



**2.1: Rendering a cloud** In the plots below, plot the values for the scenario above assuming the circles have low density values  $\sigma = \ln 2$  ( $\alpha \approx 0.5$ ).



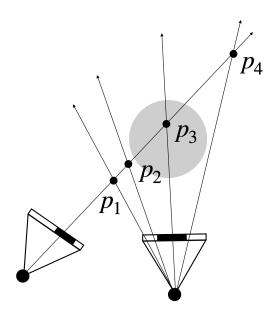
**2.2: Rendering a solid** In the plots below, plot the values for the scenario above assuming the circles have very high density values  $\sigma = 1000$ .



2.3: Analysis Explain which quantity accounts for occlusion in 3D, and how it accomplishes this.

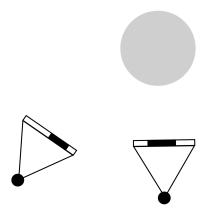
#### 3 Multiview in Flatland

The diagram below shows 2 cameras, each observing a circle in 2D, which projects to a black stripe in their images. On the right are illustrated 4 points in 2D along with their projections into the two cameras.



**3.1: 4-point NeRF.** Based on these 4 points, come up with an assignment of density and color to each point  $p_i$  which satisfies the input images.

**3.2:** Where's the density? Extending the logic from 3.1, indicate in the diagram below *all possible* region over which the density in the scene could lie. (Hint: It's larger than the circle.)



**3.3:** Adding a new view Based on the existing 2 views, where should I take a new image to give me the most information about where density lives in the scene? Draw the new view and sketch the new region of density.

